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 - Bound states?
 - Simplify: Just Higgs and W/Z

The Higgs sector as a gauge theory

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$$L = -\frac{1}{4} W_{\mu\nu}^a W_a^{\mu\nu}$$

$$W_{\mu\nu}^a = \partial_\mu W_\nu^a - \partial_\nu W_\mu^a$$



- **Ws** W_μ^a

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- Coupling g and some numbers f^{abc}

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- Ws

$$W_\mu^a$$

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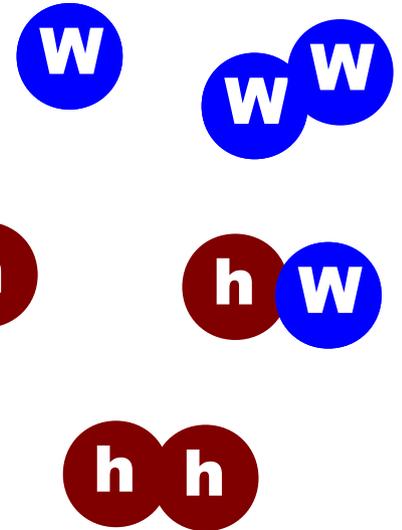
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- Ws** W_μ^a

- Higgs** h_i

- No QED: Ws and Zs are degenerate

- Couplings g , v , λ and some numbers f^{abc} and t_a^{ij}



Symmetries

$$L = -\frac{1}{4} W_{\mu\nu}^a W_a^{\mu\nu} + (D_\mu^{ij} h^j)^\dagger D_{ik}^\mu h_k + \lambda (h^a h_a^\dagger - v^2)^2$$

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- Local SU(2) gauge symmetry

- Invariant under arbitrary gauge transformations $\phi^a(x)$

$$W_\mu^a \rightarrow W_\mu^a + (\delta_b^a \partial_\mu - gf_{bc}^a W_\mu^c) \phi^b$$

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- Global SU(2) Higgs flavor symmetry

- Acts as right-transformation on the Higgs field only

$$W_\mu^a \rightarrow W_\mu^a \qquad h_i \rightarrow h_i + a^{ij} h_j + b^{ij} h_j^*$$

Parameters

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- Non-perturbative: Simulate Higgs+W [Maas'12]

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- Non-perturbative: Simulate Higgs+W [Maas'12]
 - Physical W/Higgs mass ratio
 - Good comparison to perturbation theory
 - Error at least of order W-Z mass splitting
 - Close to the transition to QCD-like behavior
- Different (bare) parameters: Talk of Mark Wurtz
 - Also good agreement to standard model

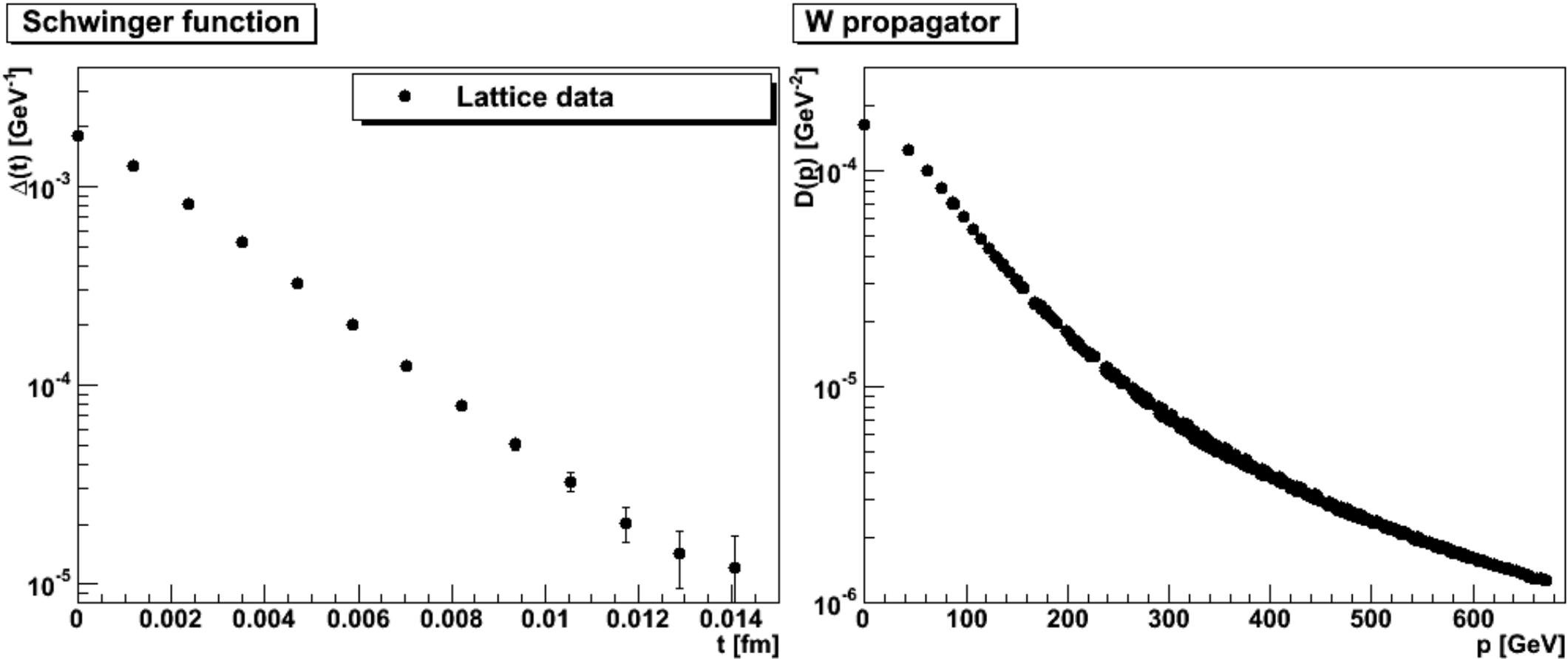
W boson

[Maas'11,'12]

- Renormalization scheme with
 $D(\mu) = 1/(\mu^2 + (80.375 \text{ GeV})^2) \wedge \mu = 80.375 \text{ GeV}$

W boson

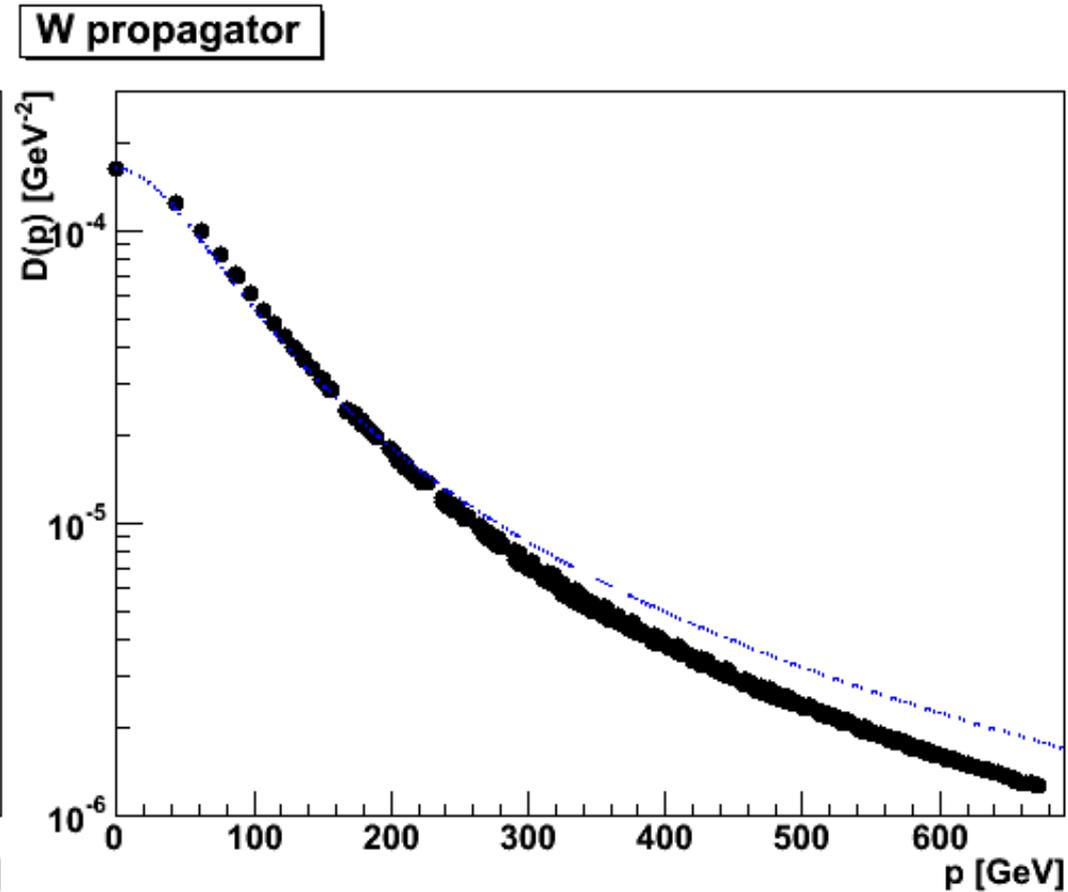
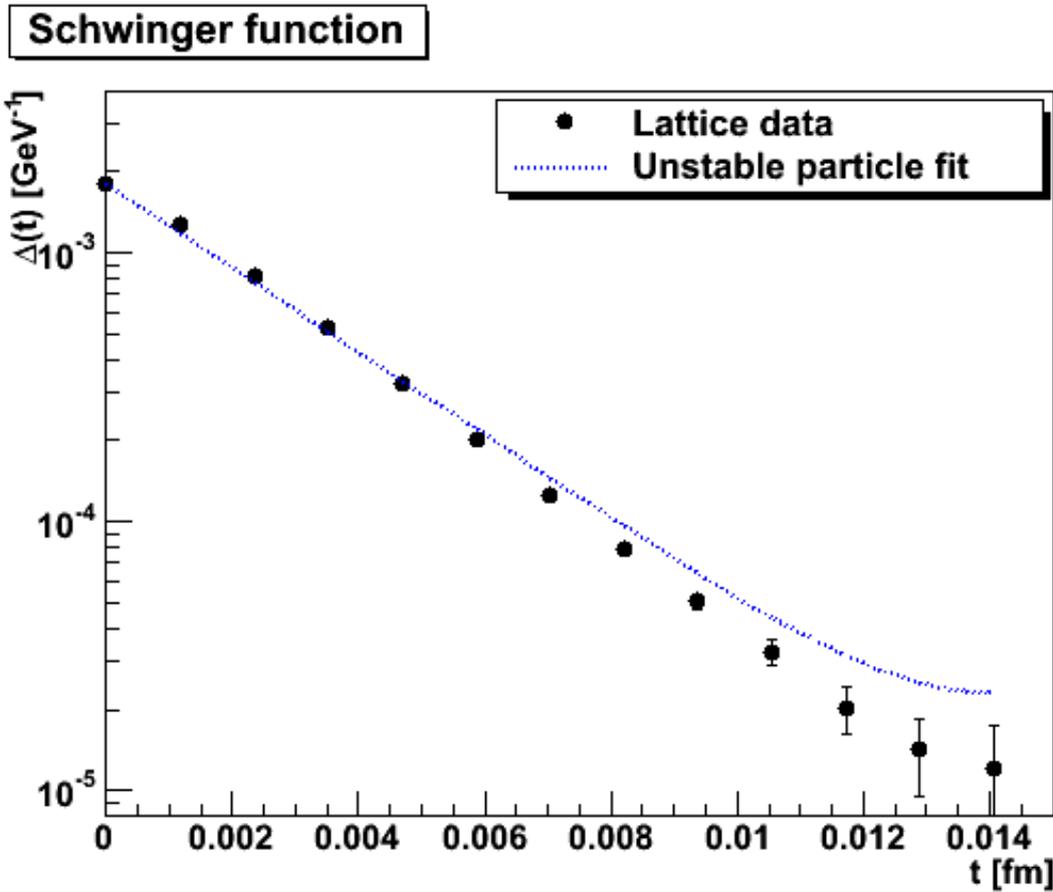
[Maas'11,'12]



- Renormalization scheme with $D(\mu) = 1/(\mu^2 + (80.375 \text{ GeV})^2) \wedge \mu = 80.375 \text{ GeV}$
- Massive-like propagator
- Dynamical mass generation

W boson

[Maas'11,'12]

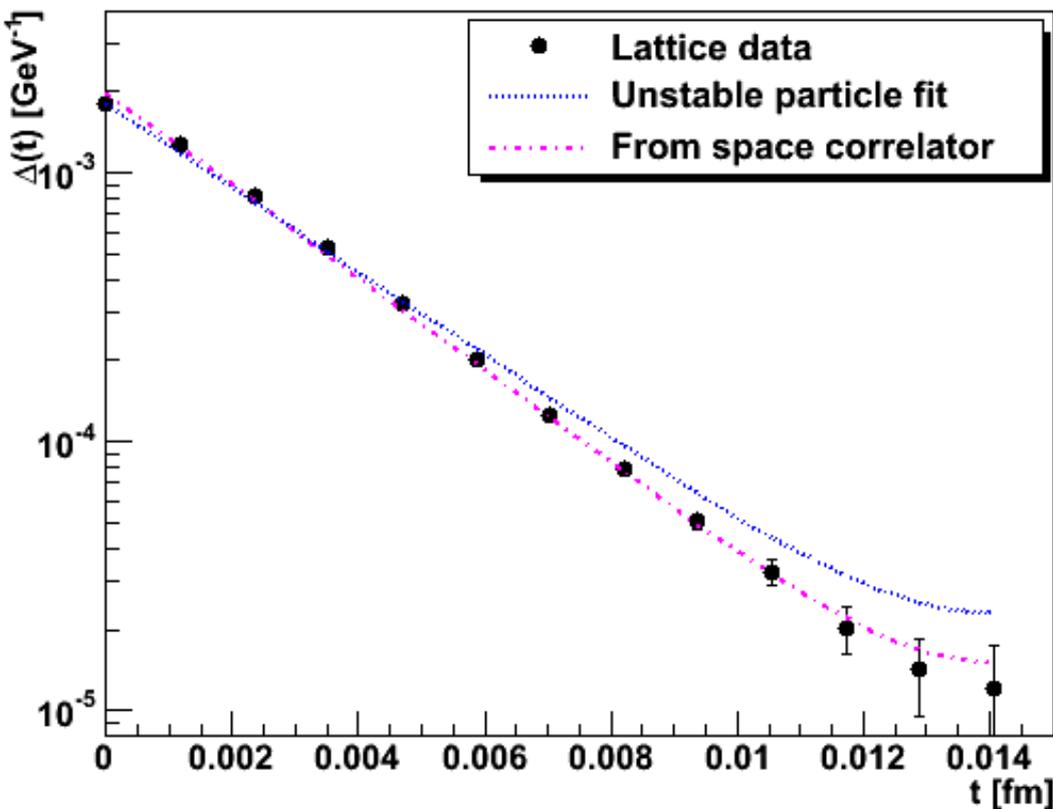


Fit type	Mass	Remark
Unstable	71.8(1) GeV	Width: 2.1(4) GeV

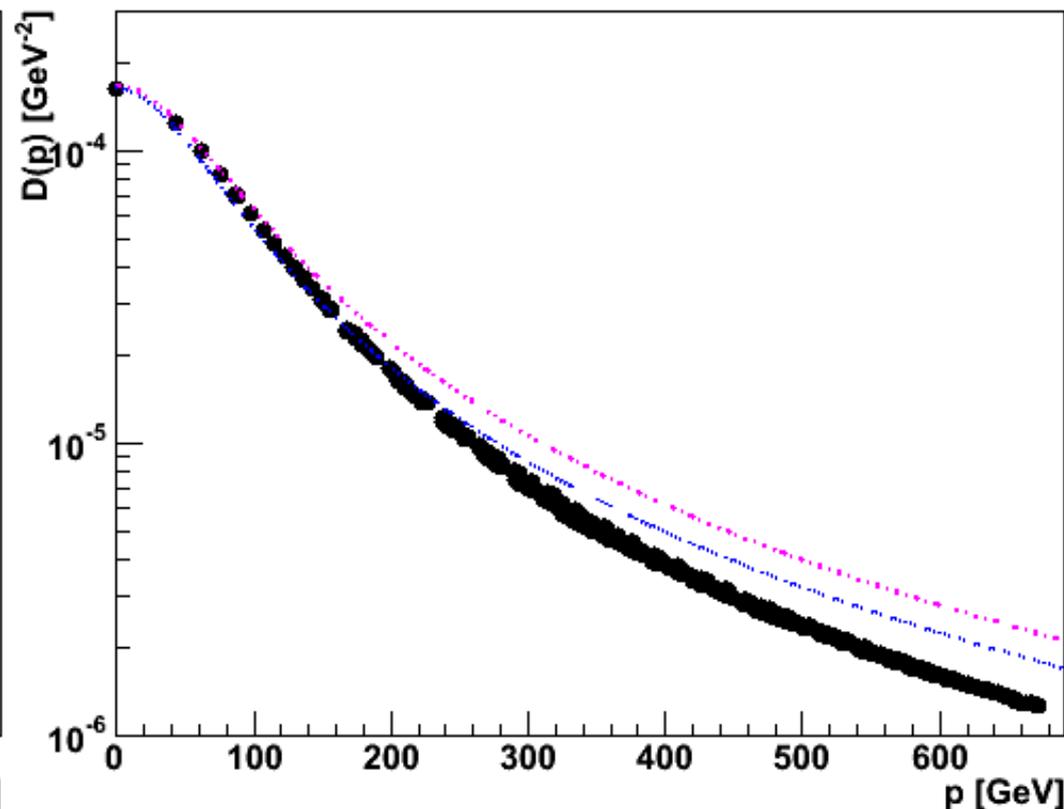
W boson

[Maas'11,'12]

Schwinger function



W propagator

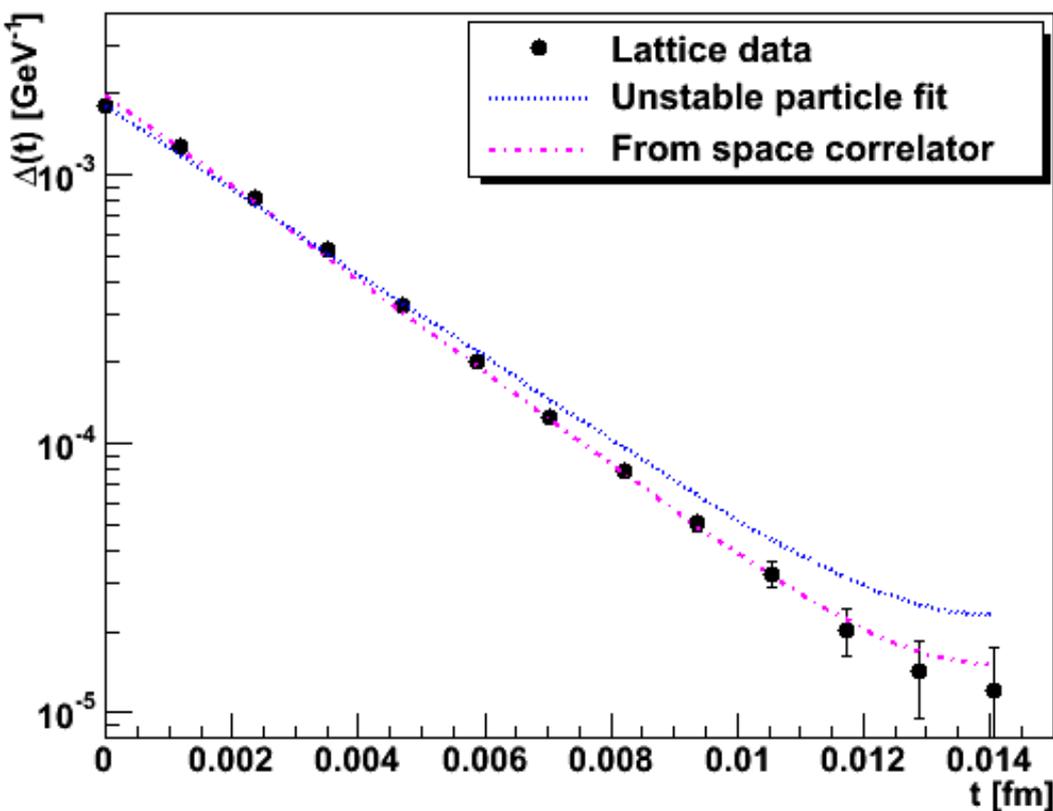


Fit type	Mass	Remark
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Configuration space	79(4) GeV	

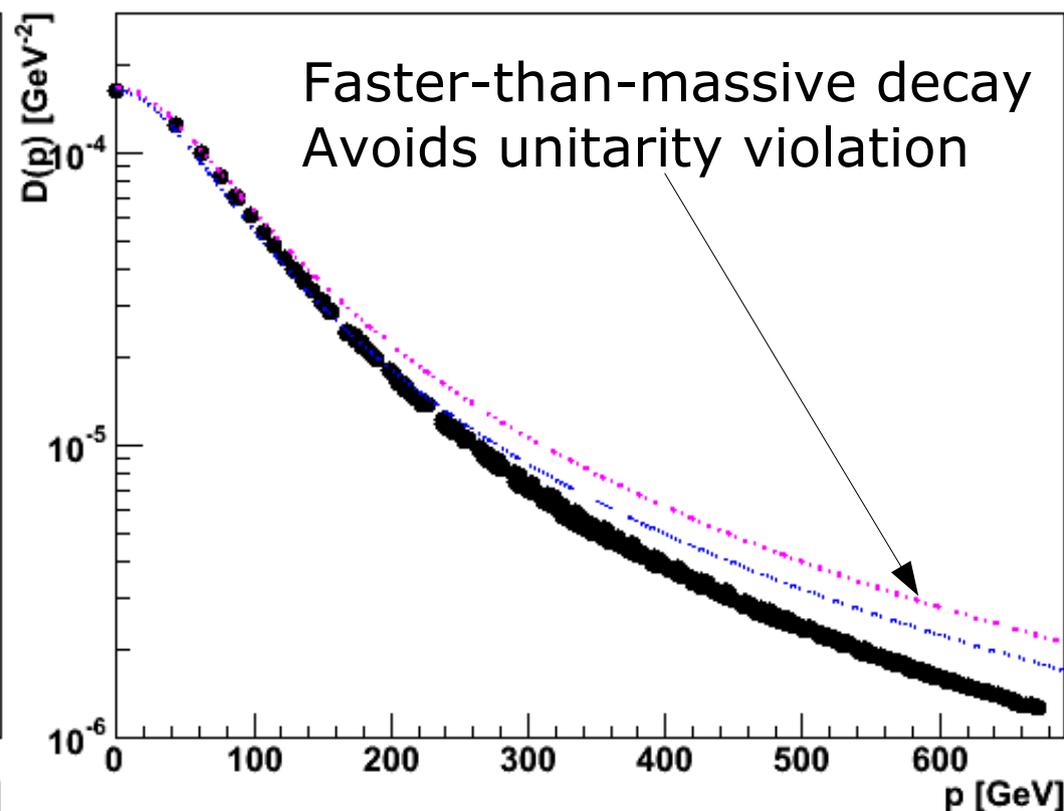
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Higgs boson

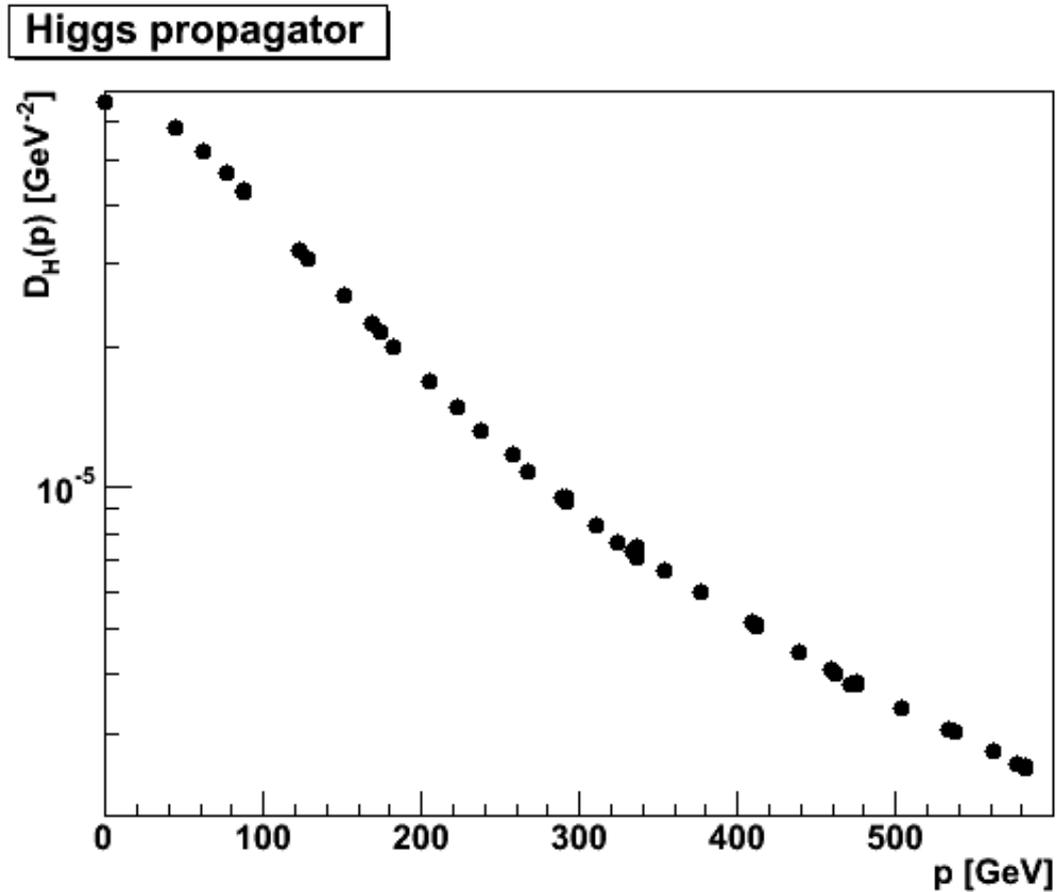
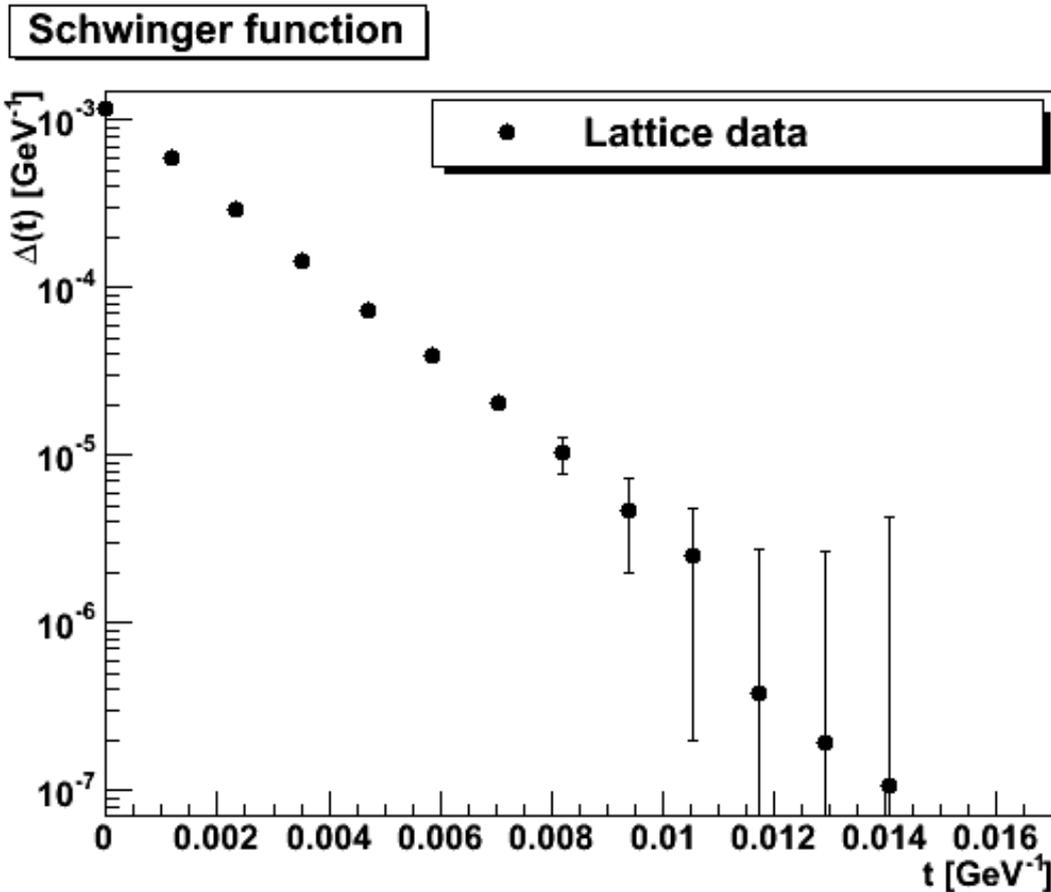
[Maas'11,'12]

- Renormalization scheme with

$$\begin{aligned}D(\mu) &= D^{tl}(\mu) \\ D(\mu)' &= D^{tl}(\mu)' \\ D^{tl}(p) &= 1/(p^2 + (123 \text{ GeV})^2) \\ \mu &= 123 \text{ GeV}\end{aligned}$$

Higgs boson

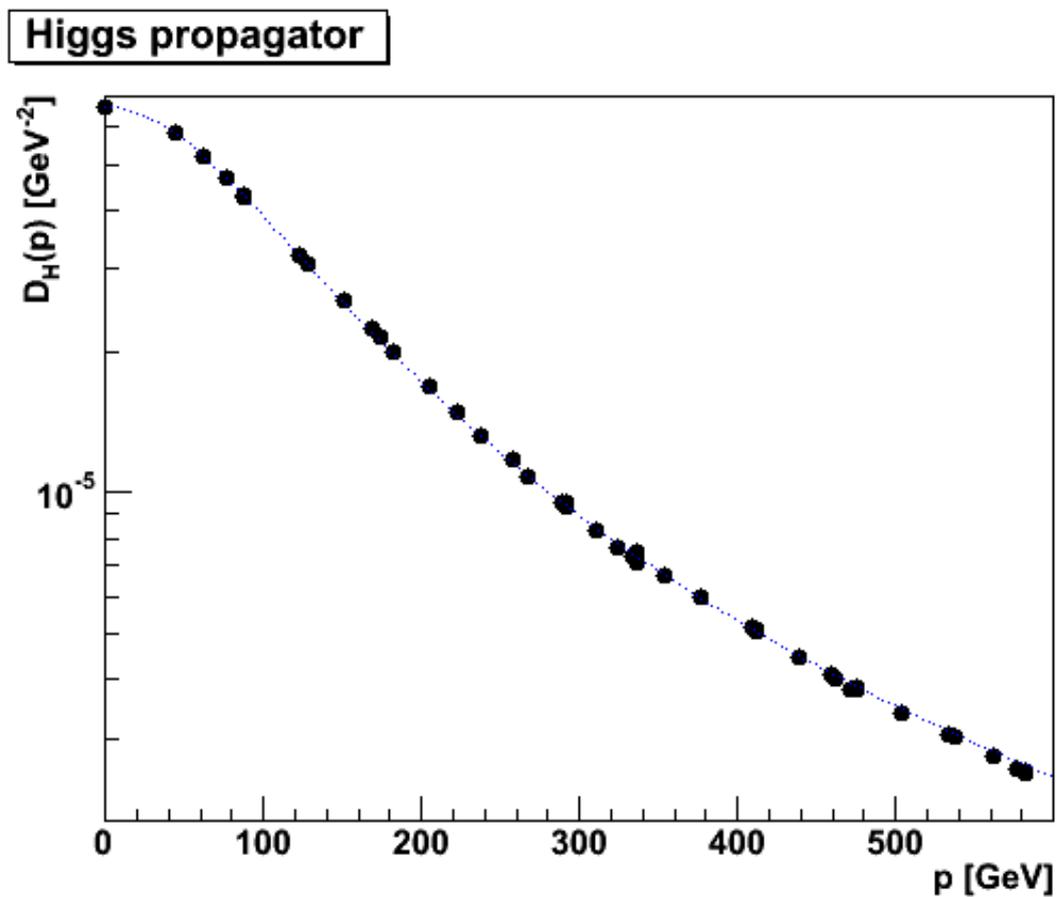
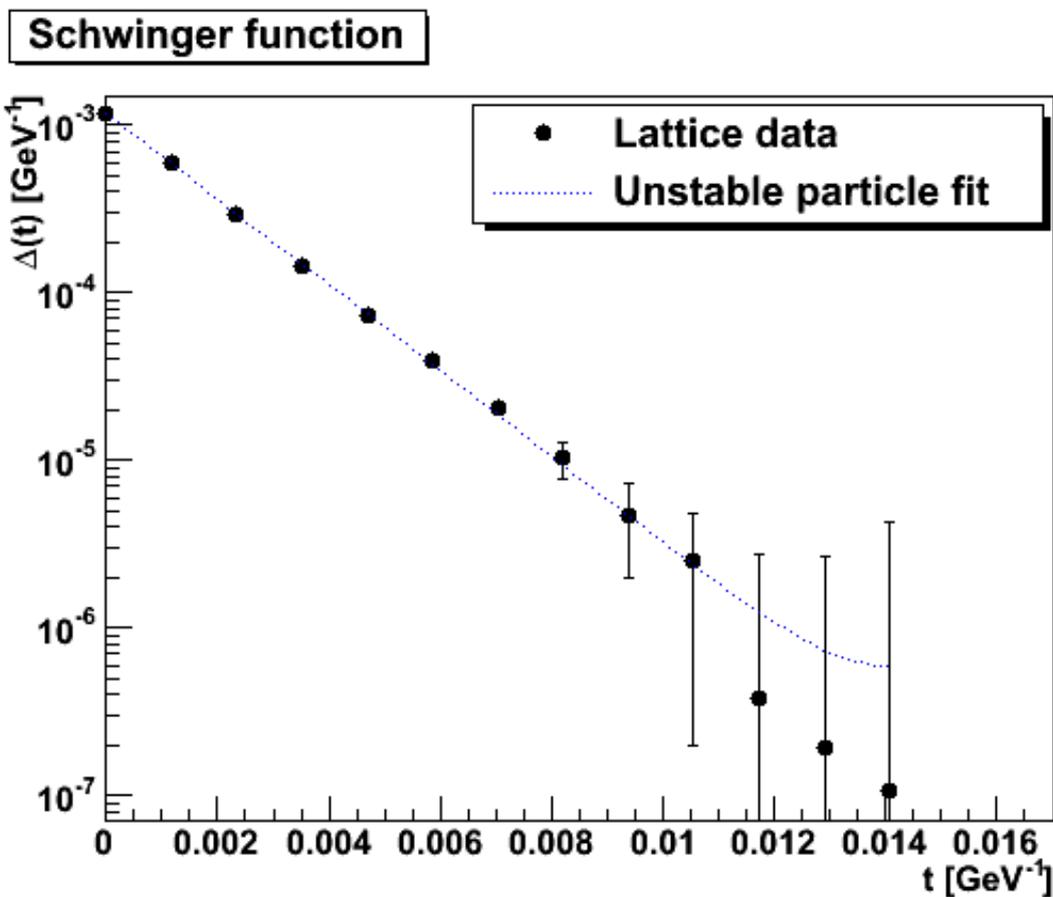
[Maas'11,'12]



- Normal propagator – normal mass

Higgs boson

[Maas'11,'12]



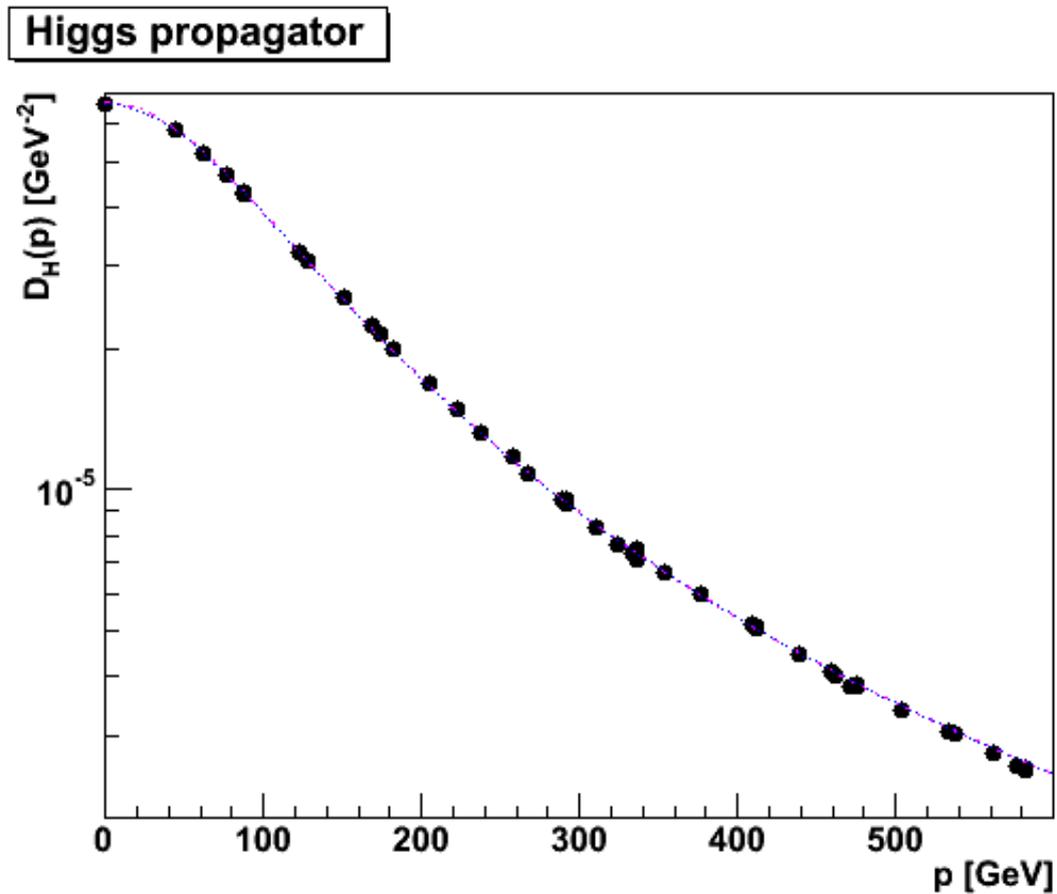
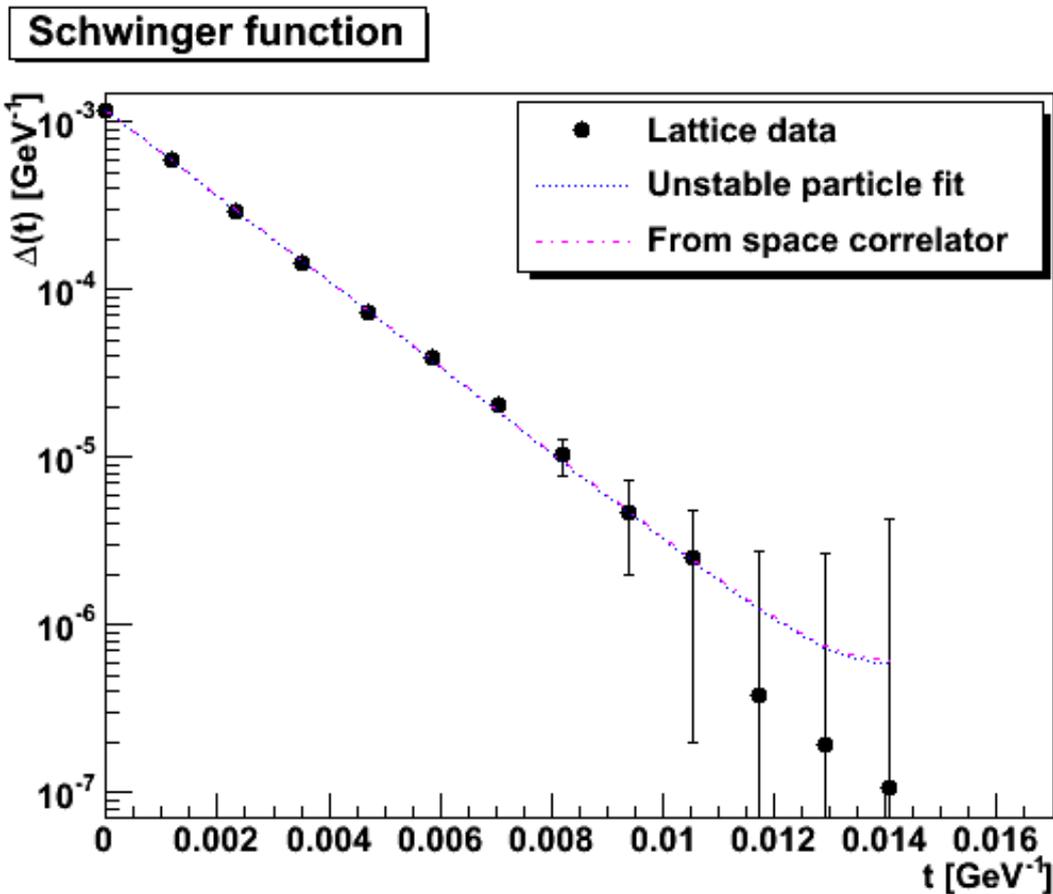
Fit type
Unstable

Pole mass
119(2) GeV

Remark
Width 1(1) GeV

Higgs boson

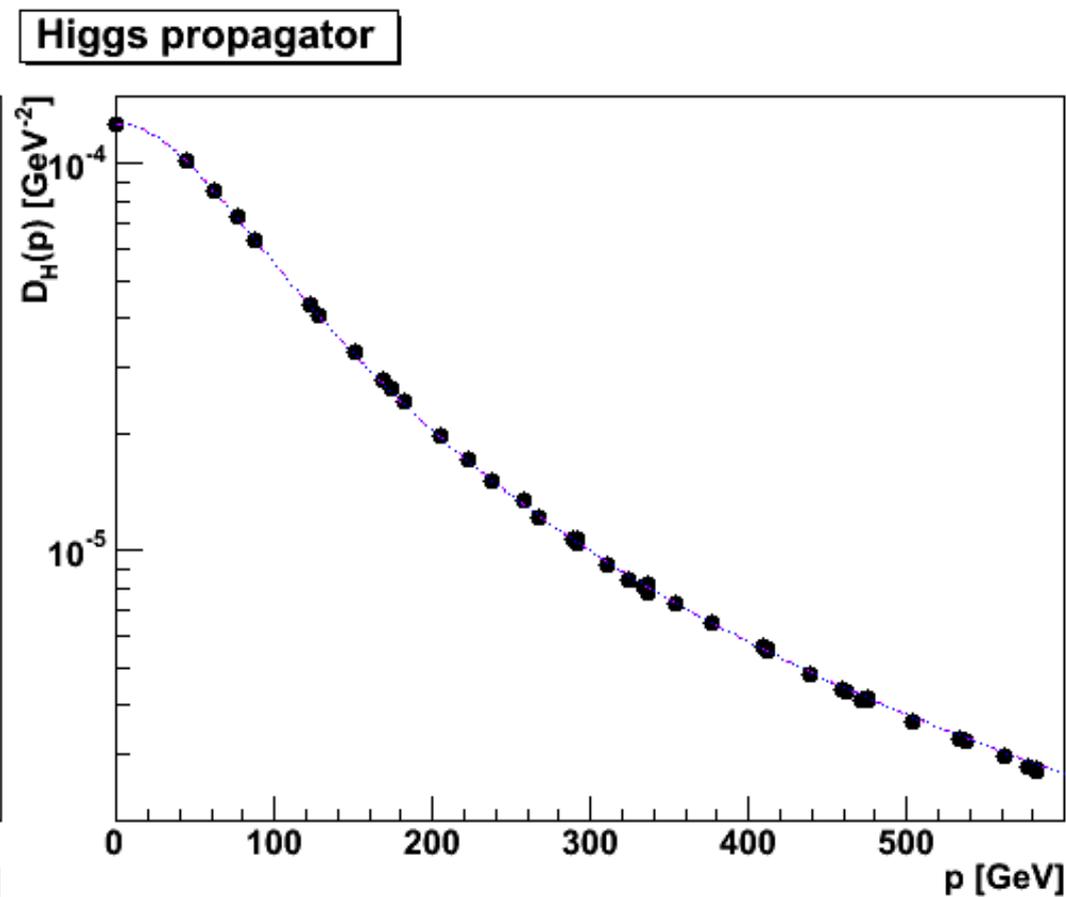
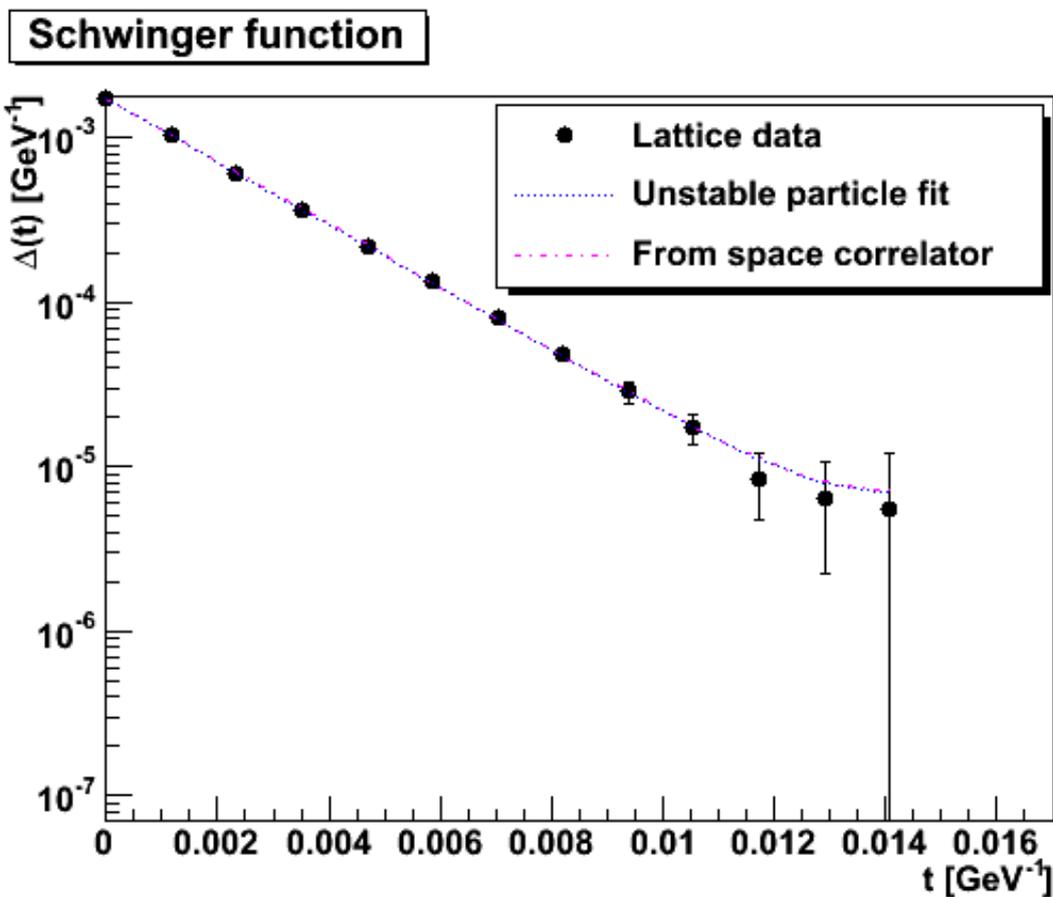
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Fit type	Pole mass	Remark
Unstable	119(2) GeV	Width 1(1) GeV
Configuration space	118(1) GeV	

Scheme dependent!

[Maas'11,'12]



Fit type	Pole mass	Remark
Unstable	86(1) GeV	Width 1(1) GeV
Configuration space	87(1) GeV	

- Different renormalization scheme with mass 90 GeV

Physical states

[Fröhlich et al.'80,
't Hooft'80,
Bank et al.'79]

- Elementary particles depend on scheme, gauge, scale...not satisfactory for a physical observable

Physical states

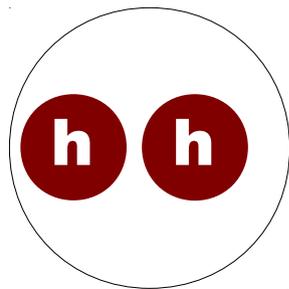
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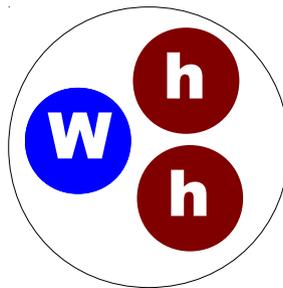
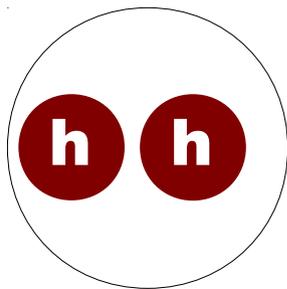
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 - Bound states: Higgs-Higgs



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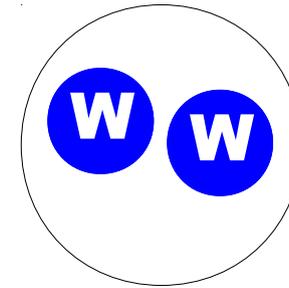
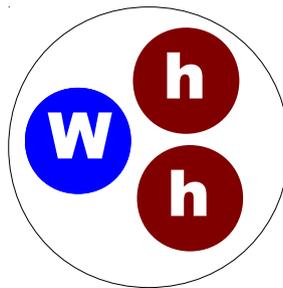
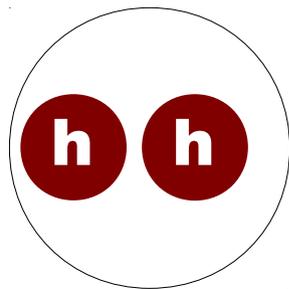
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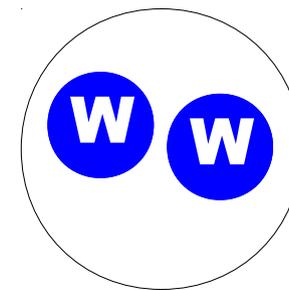
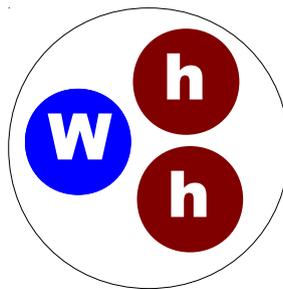
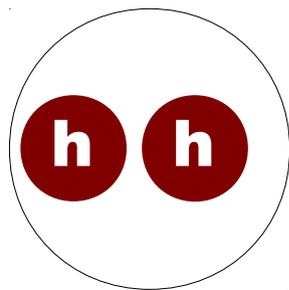
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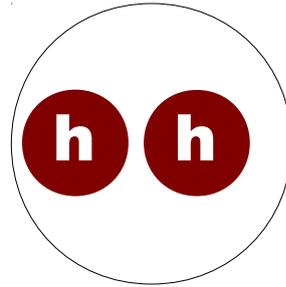
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- Lattice literature: Higgs, W, Gaugeball

Higgsonium

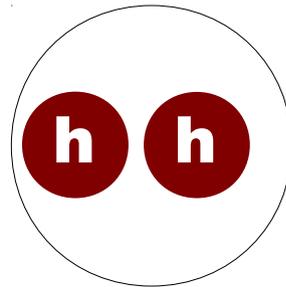
[Maas'12, Maas et al.'12]



- Simplest 0^{++} bound state $h^+(x)h(x)$

Higgsonium

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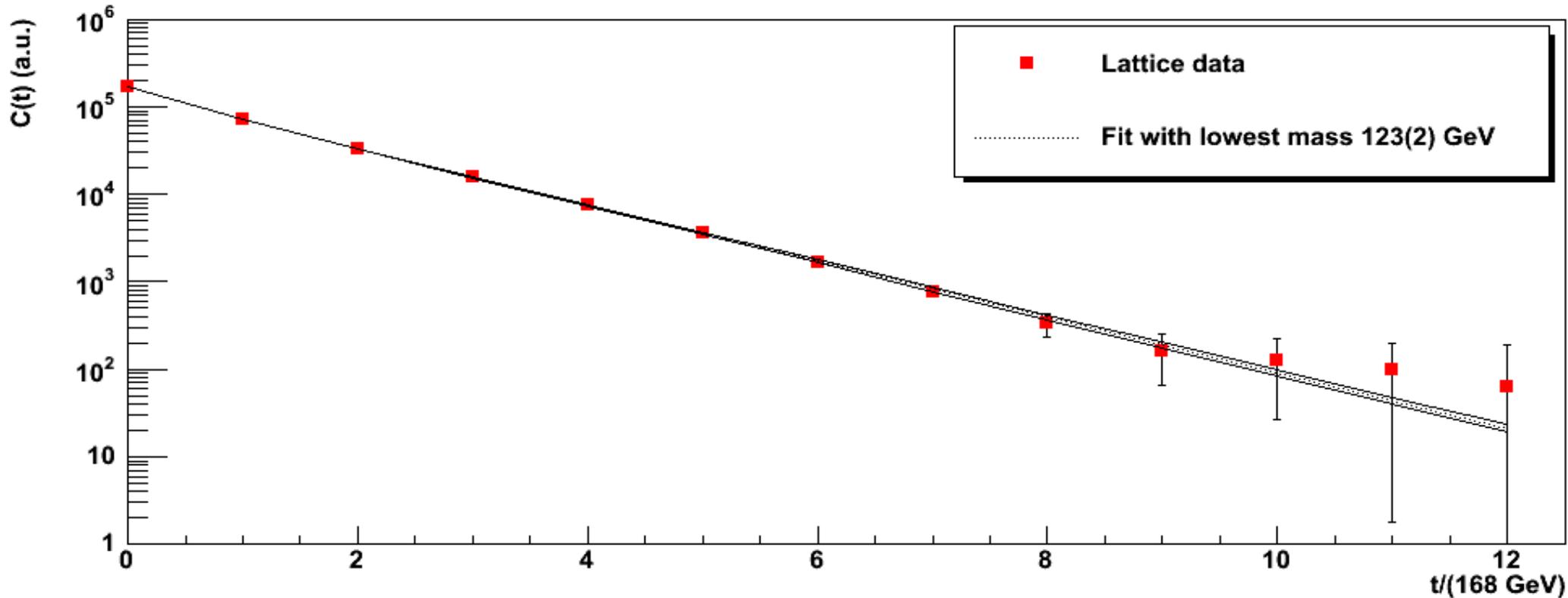


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 - No weak or flavor charge

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Higgsonium



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 - Mass is about 123 GeV

Mass relation - Higgs

- Higgsonium: 123 GeV

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[Fröhlich et al.'80]

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[Fröhlich et al.'80]

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- Deeply-bound relativistic state
 - Mass defect \sim constituent mass

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- Deeply-bound relativistic state
 - Mass defect \sim constituent mass
 - Cannot describe with quantum mechanics

Mass relation - Higgs

[Fröhlich et al.'80
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- Coincidence? No.

- Duality between elementary states and bound states

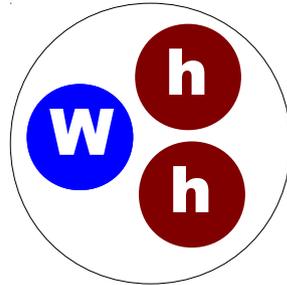
[Fröhlich et al.'80]

$$\langle (h^\dagger h)(x)(h^\dagger h)(y) \rangle \stackrel{h=v+\eta}{\approx} \text{const.} + \langle h^\dagger(x)h(y) \rangle + O(\eta^3)$$

- Same poles to leading order
- Deeply-bound relativistic state
 - Mass defect \sim constituent mass
 - Cannot describe with quantum mechanics
 - Very different from QCD bound states

Isvector-vector state

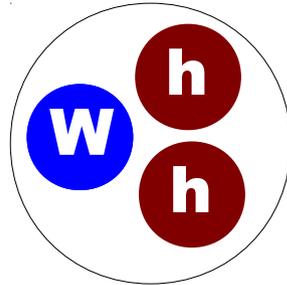
[Maas'12, Maas et al.'12]



- Vector state with operator $tr t^a \frac{h^+}{\sqrt{h^+ h}} D_u \frac{h}{\sqrt{h^+ h}}$

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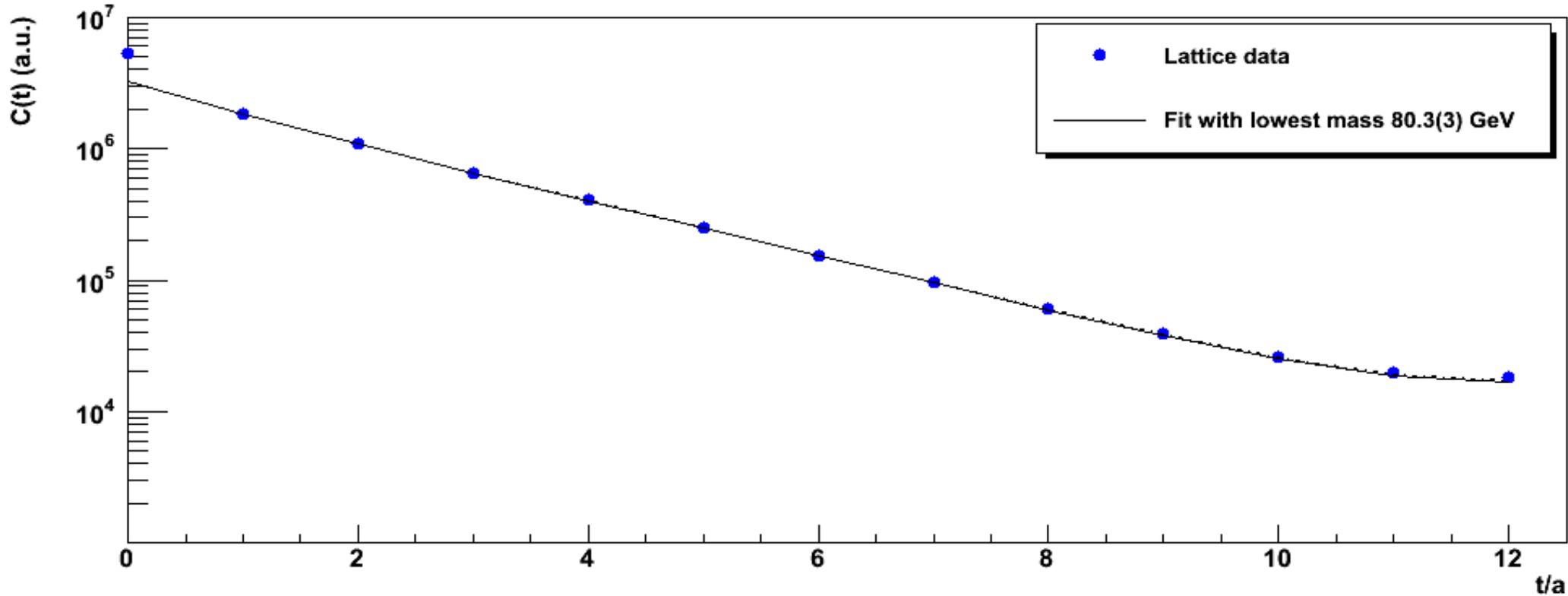


- Vector state with operator $tr t^a \frac{h^+}{\sqrt{h^+ h}} D_u \frac{h}{\sqrt{h^+ h}}$
 - Only in a Higgs phase close to a simple particle
 - Higgs-flavor triplet

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[Maas'12, Maas et al.'12]

1^- correlator



- Vector state with operator $tr t^a \frac{h^+}{\sqrt{h^+ h}} D_u \frac{h}{\sqrt{h^+ h}}$
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 - Mass about 80 GeV

Mass relation - W

[Fröhlich et al.'80
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 - At least for a light Higgs

Consequences I – W and Higgs

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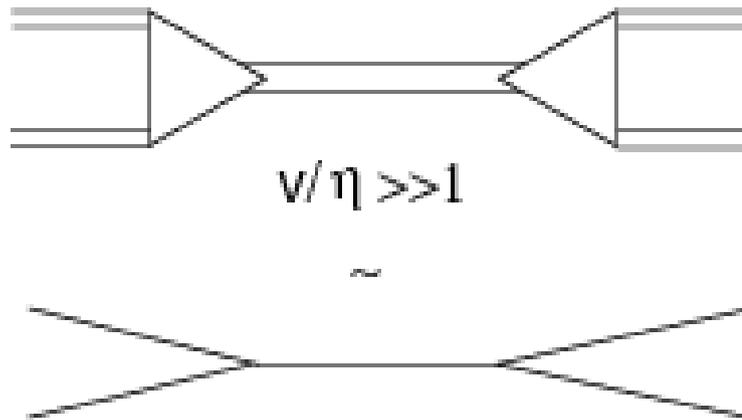
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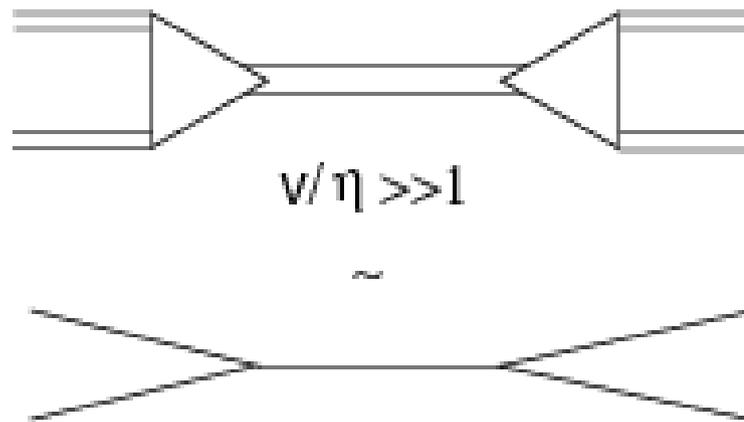
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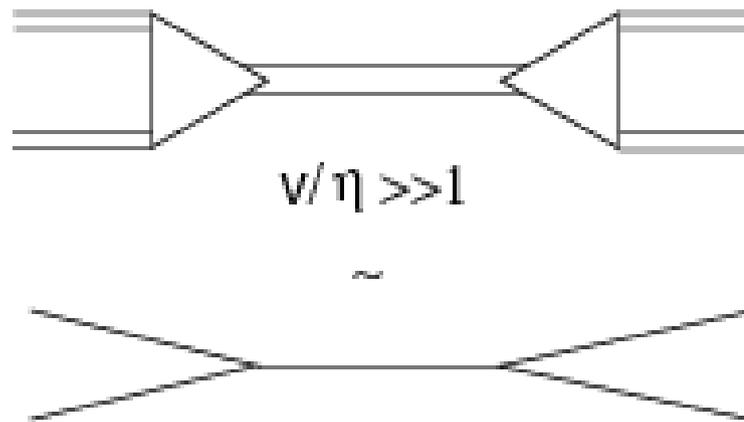


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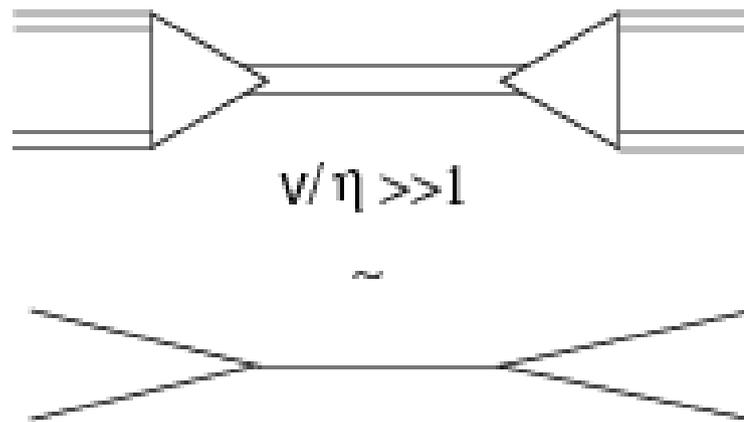


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Consequences II – Excited states

Spectrum

PRELIMINARY

[Maas et al. Unpublished,'12]



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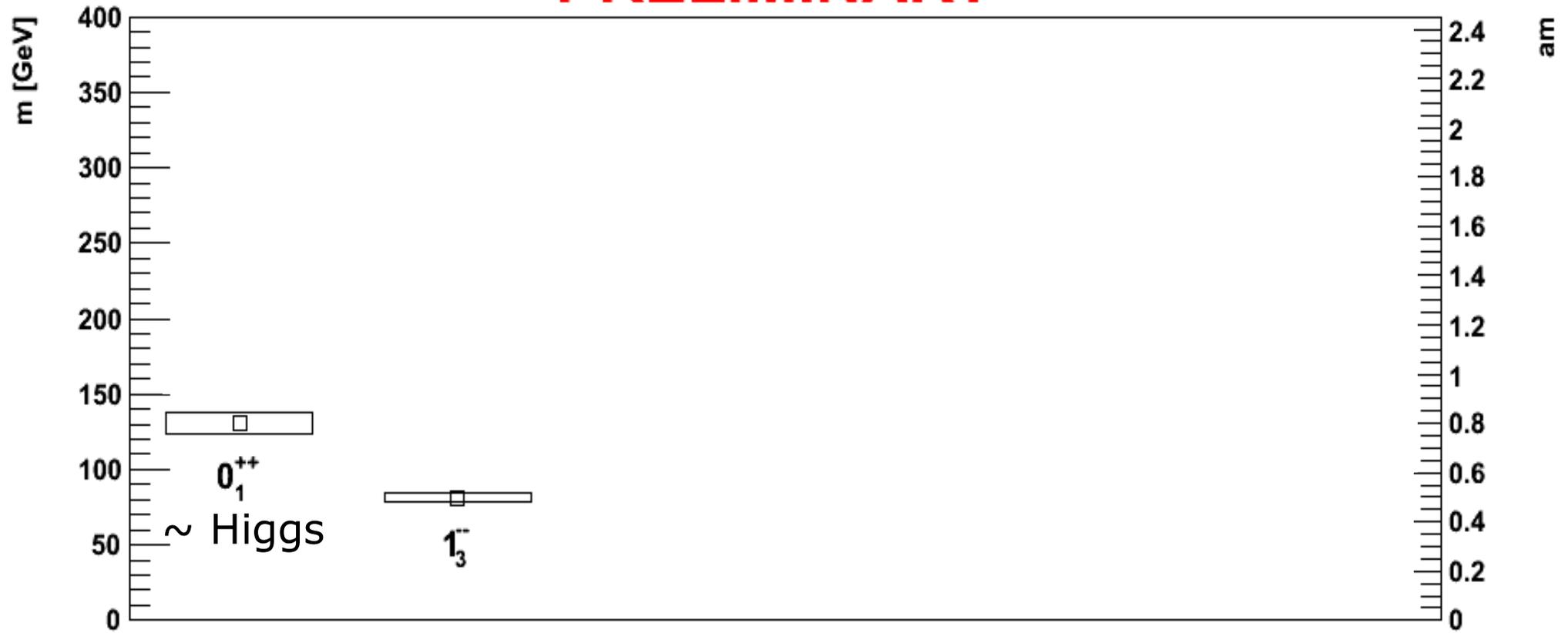


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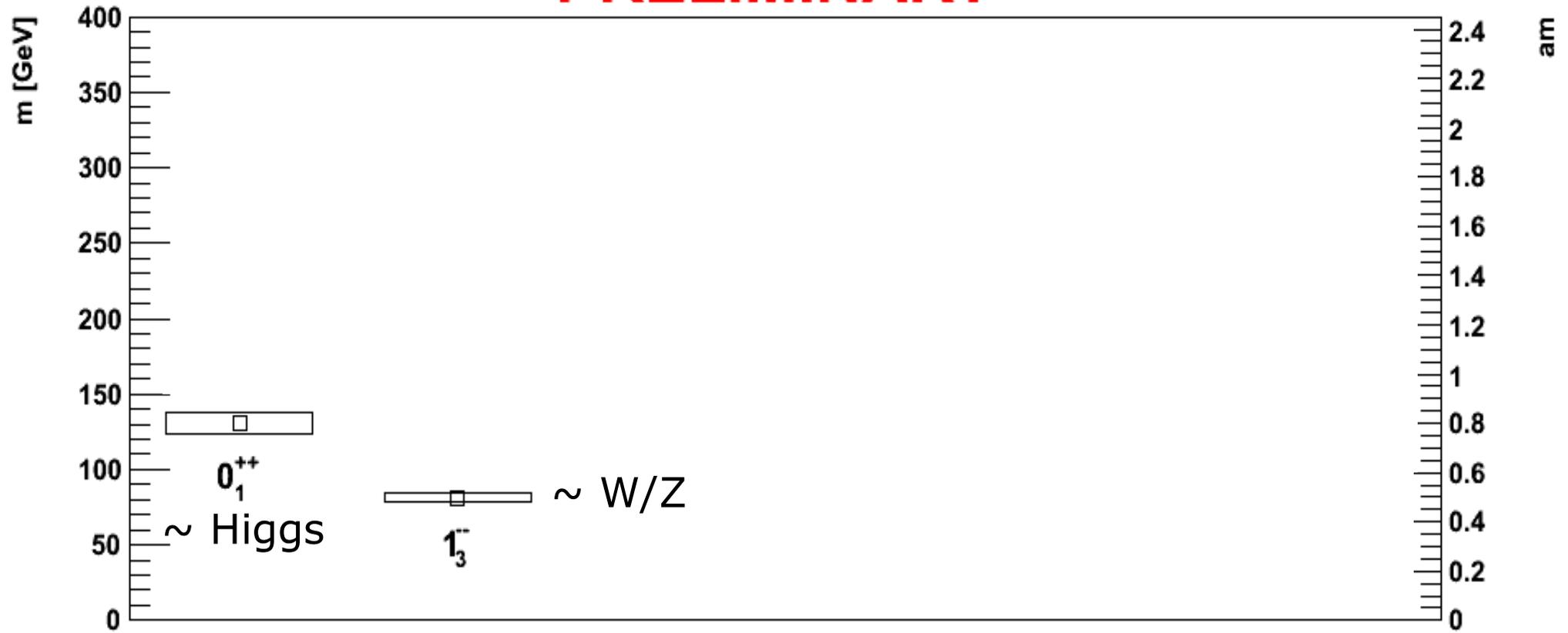


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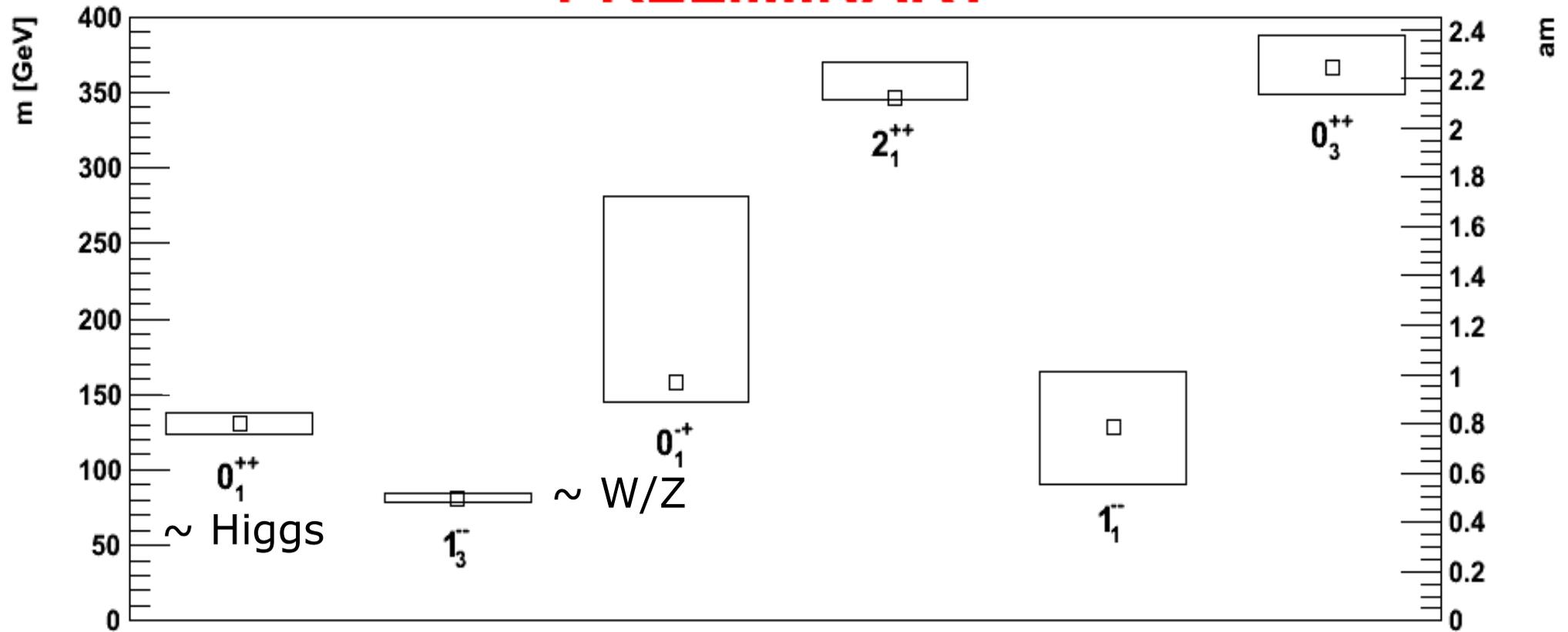


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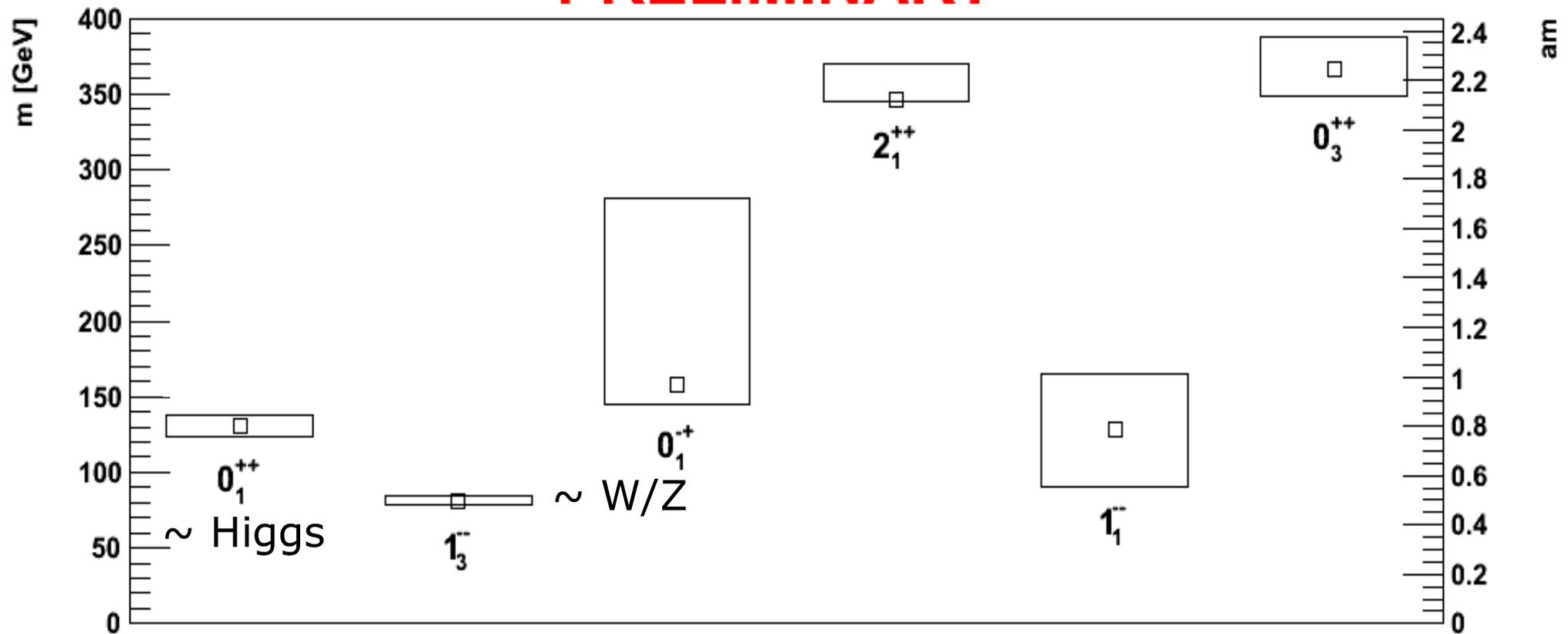
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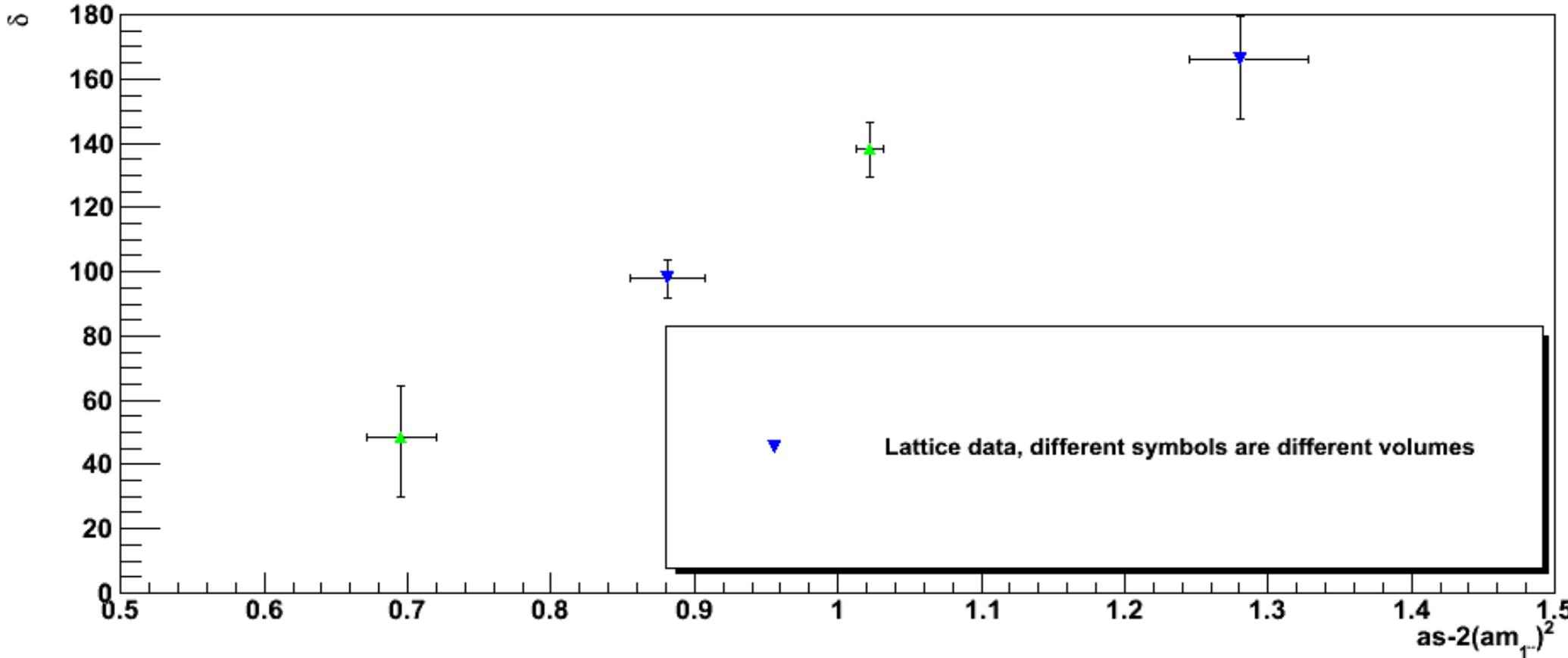
Consequences II – Excited states

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[Maas et al. Unpublished]

Channel $0^{++} \rightarrow 2\ 1^{-}$ decay channel

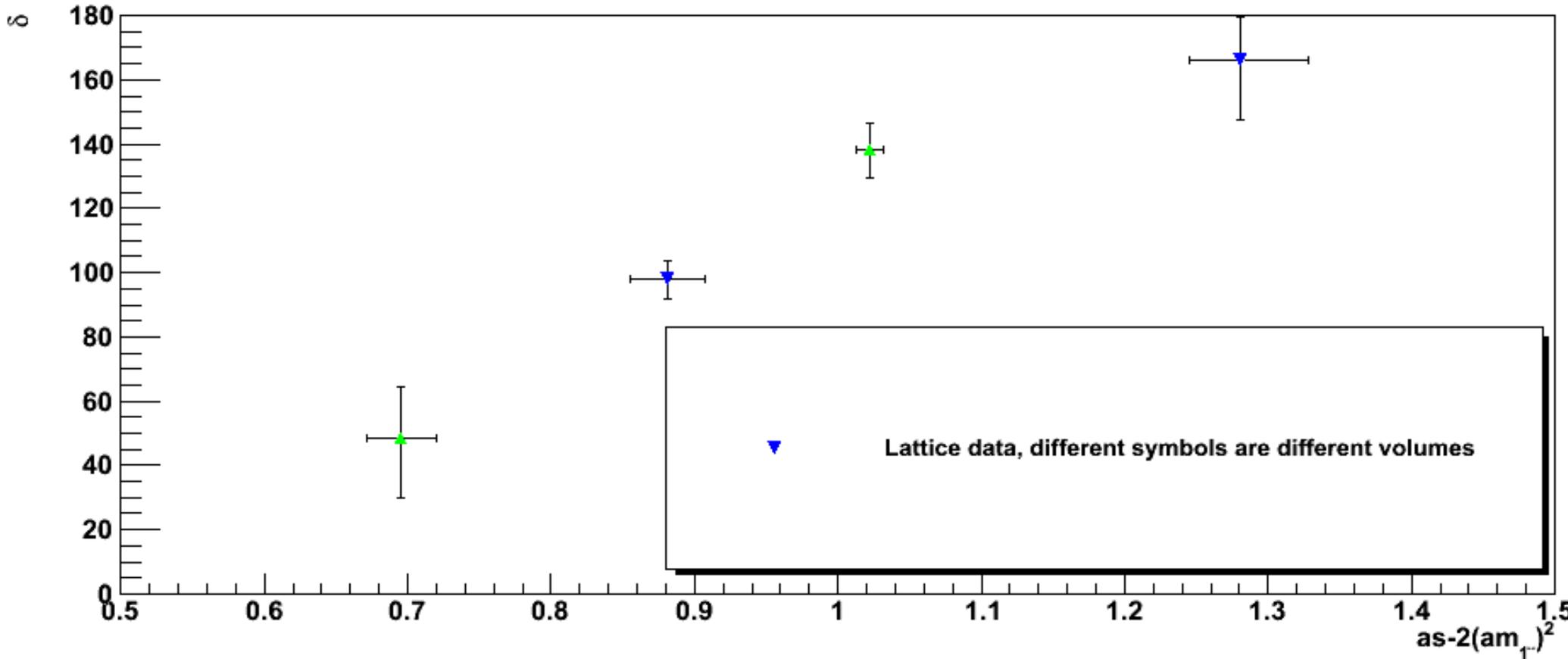


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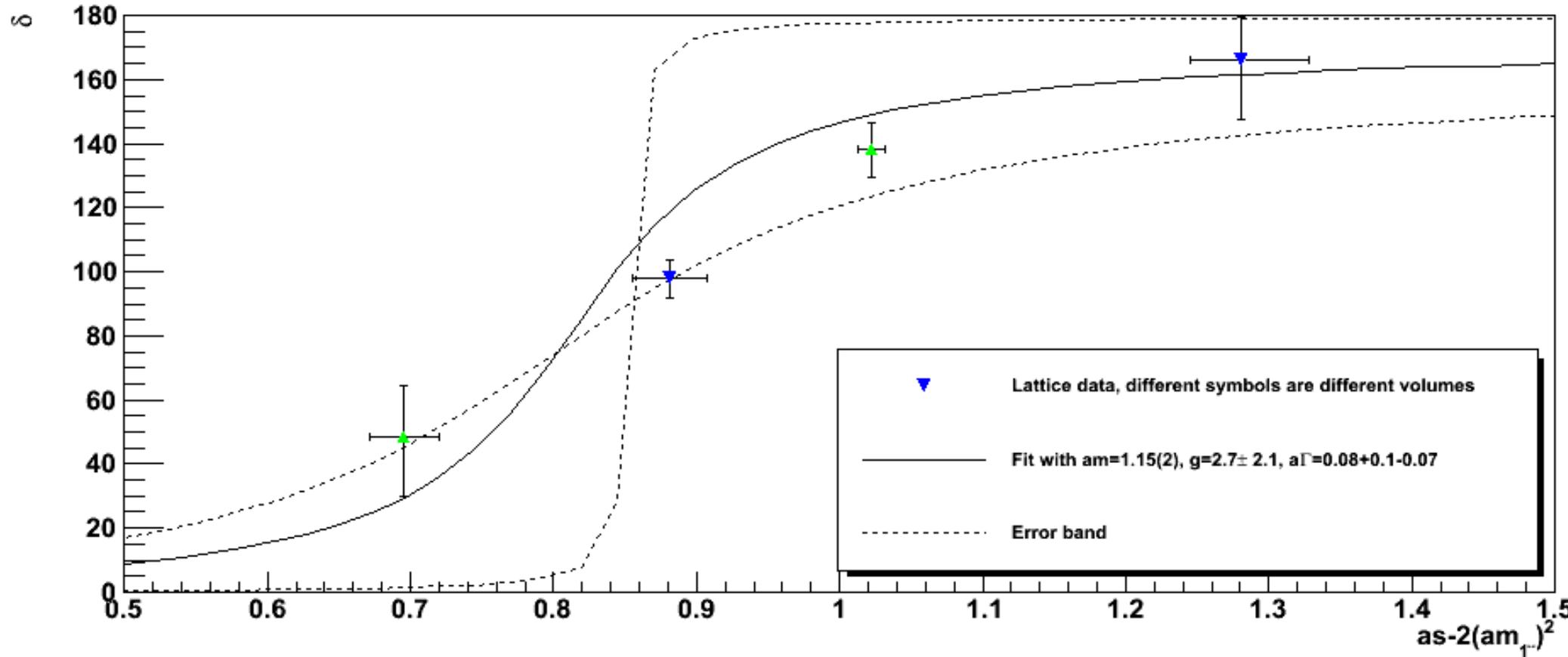


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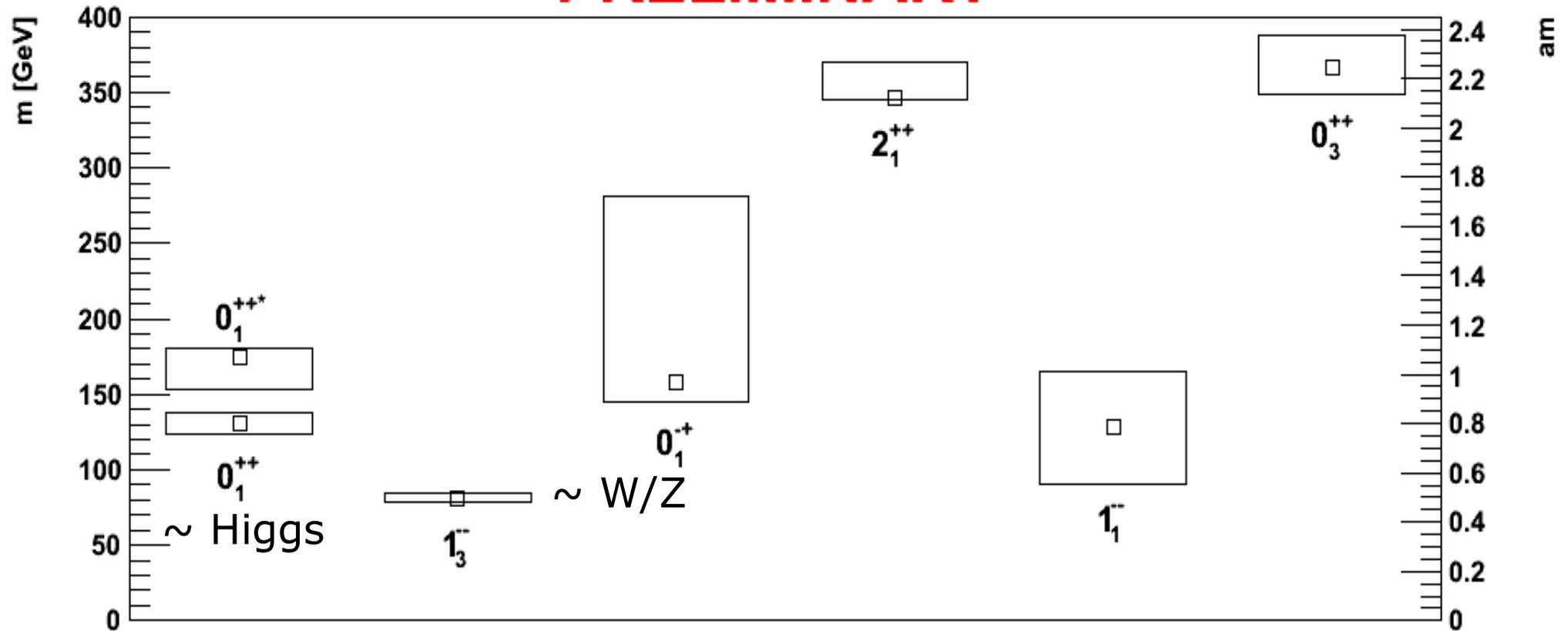
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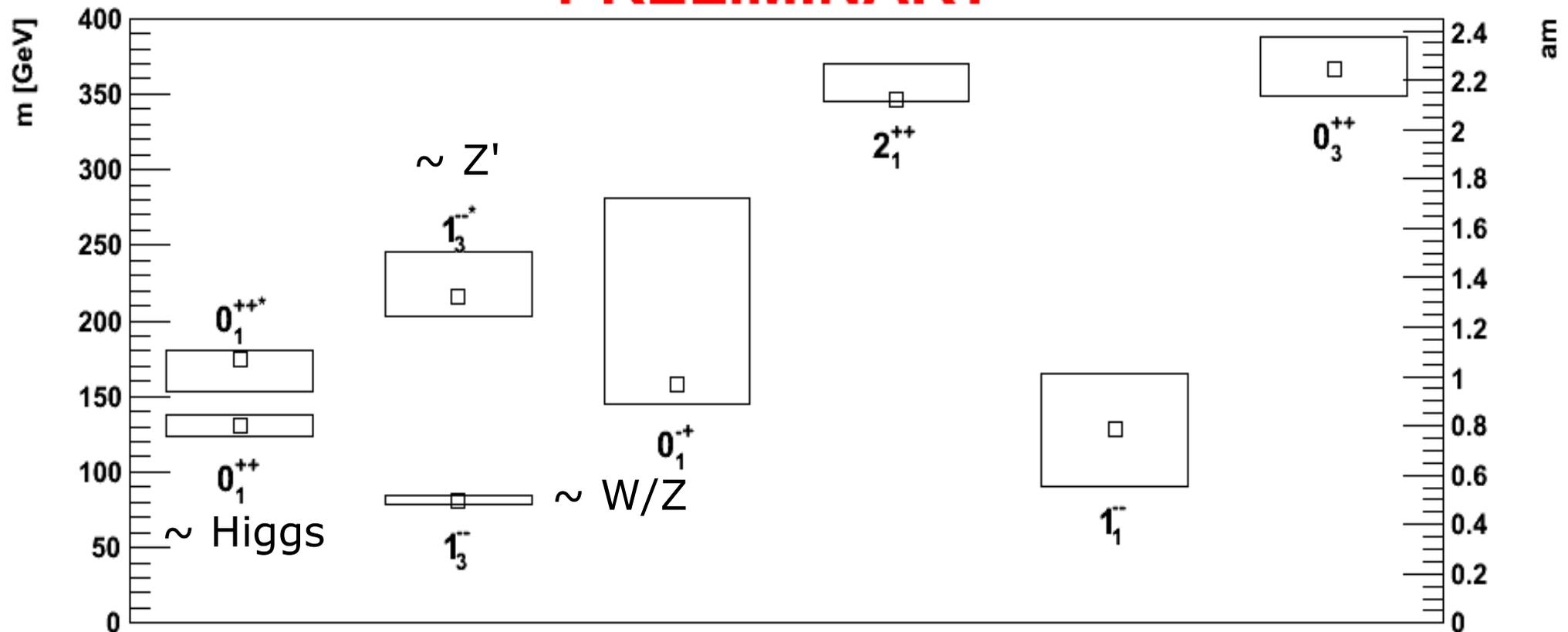
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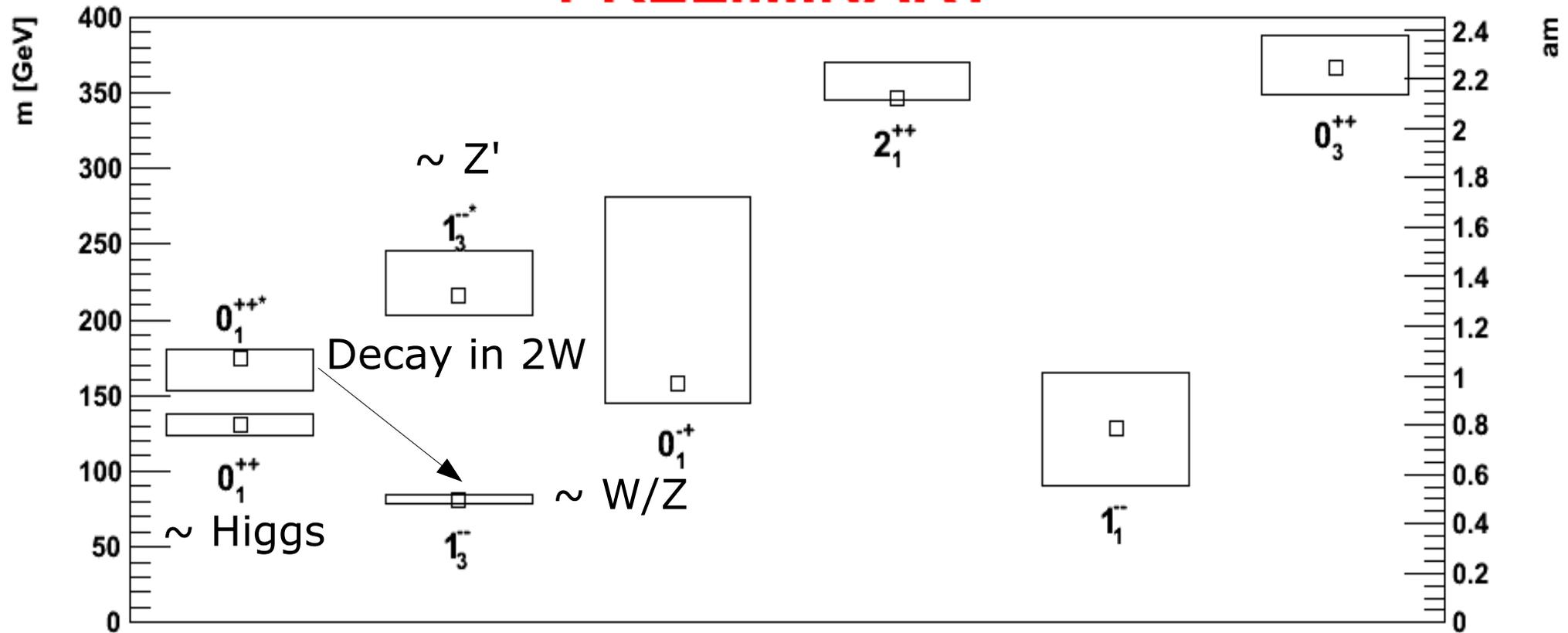
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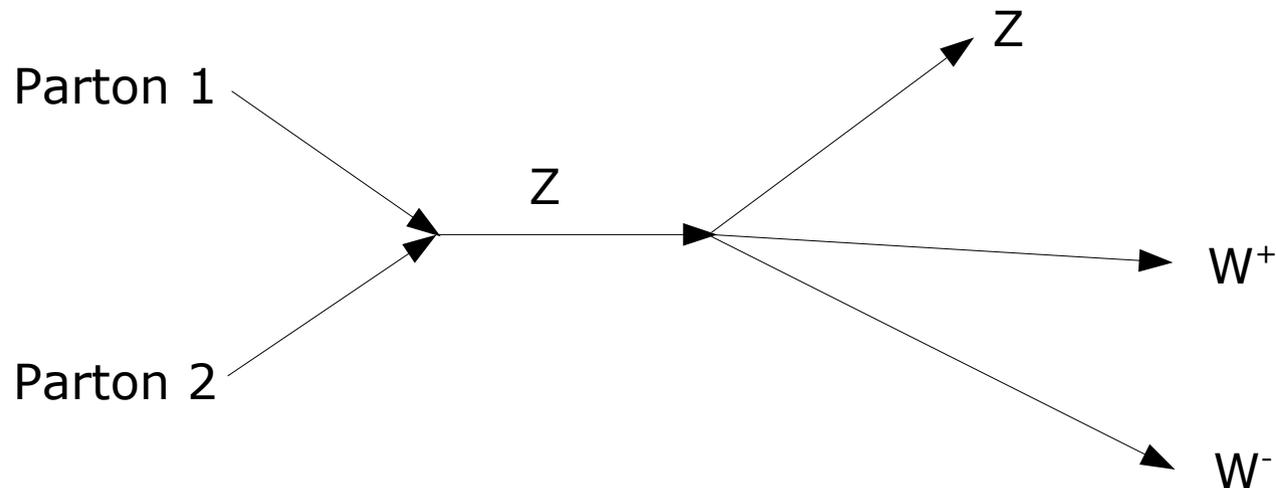
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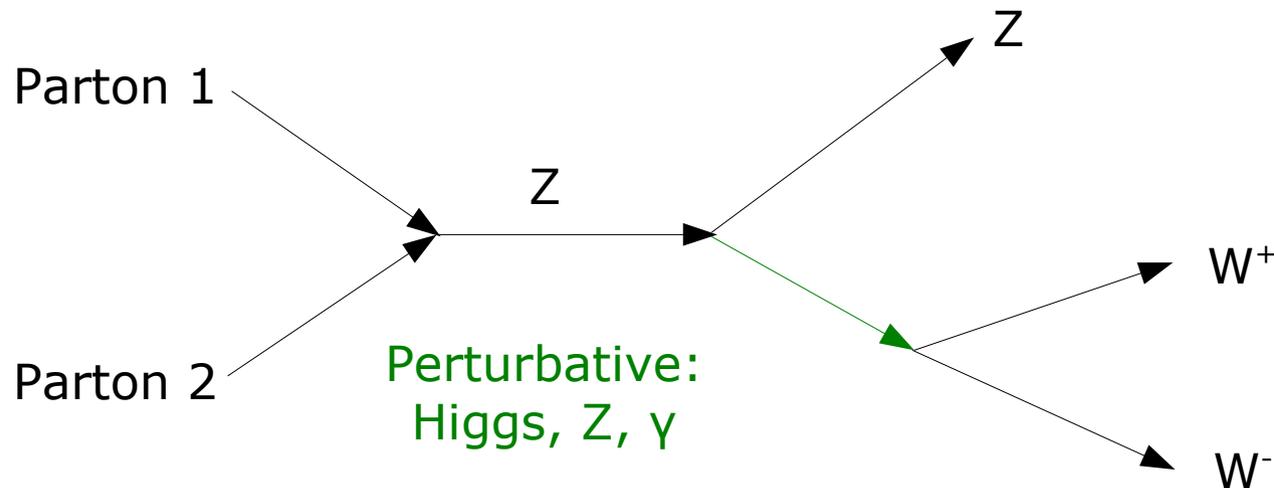


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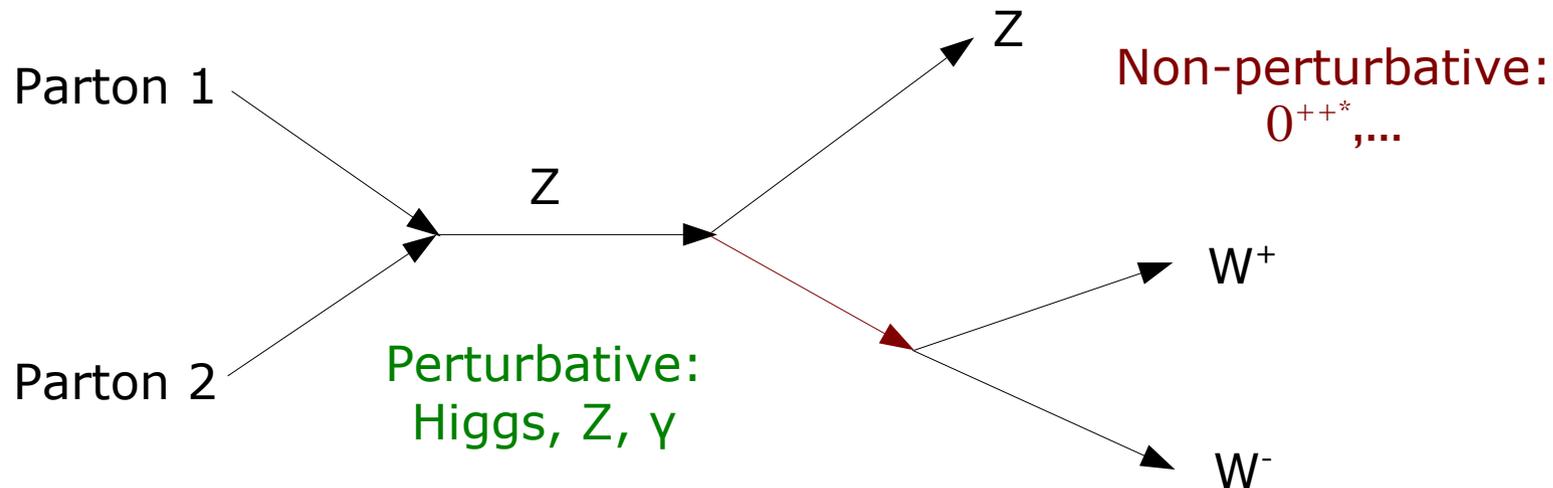


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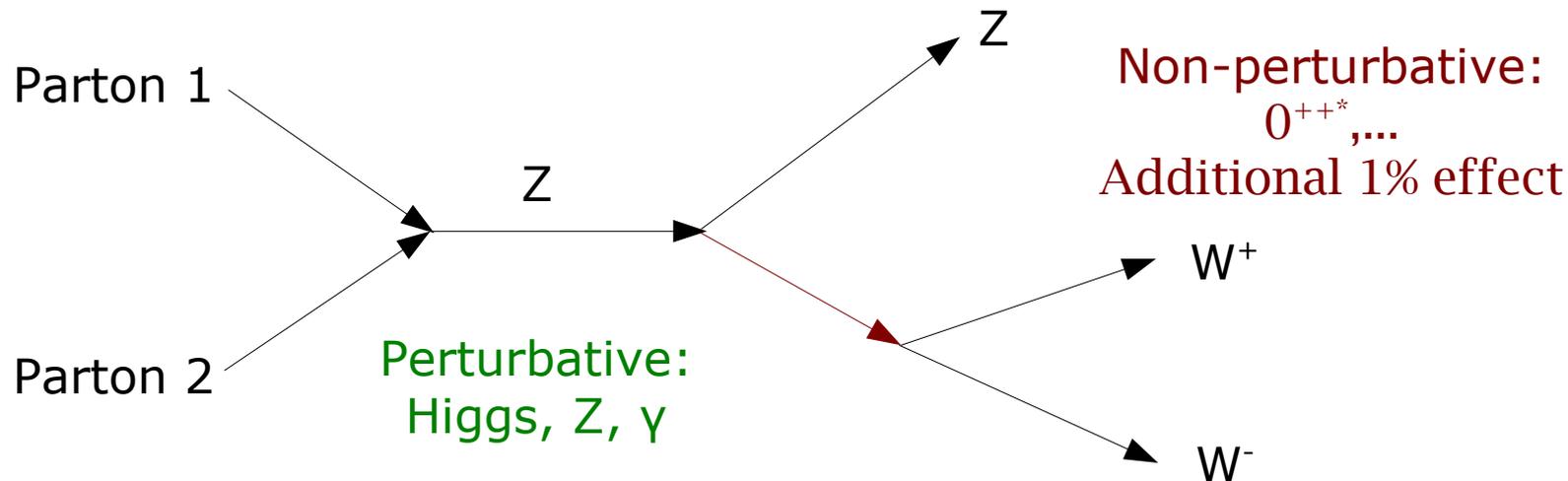


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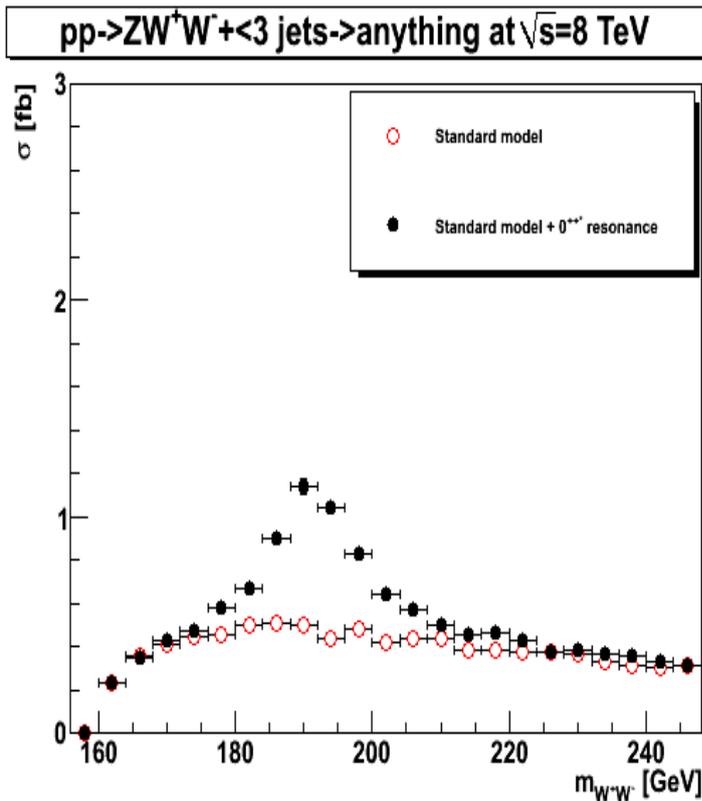


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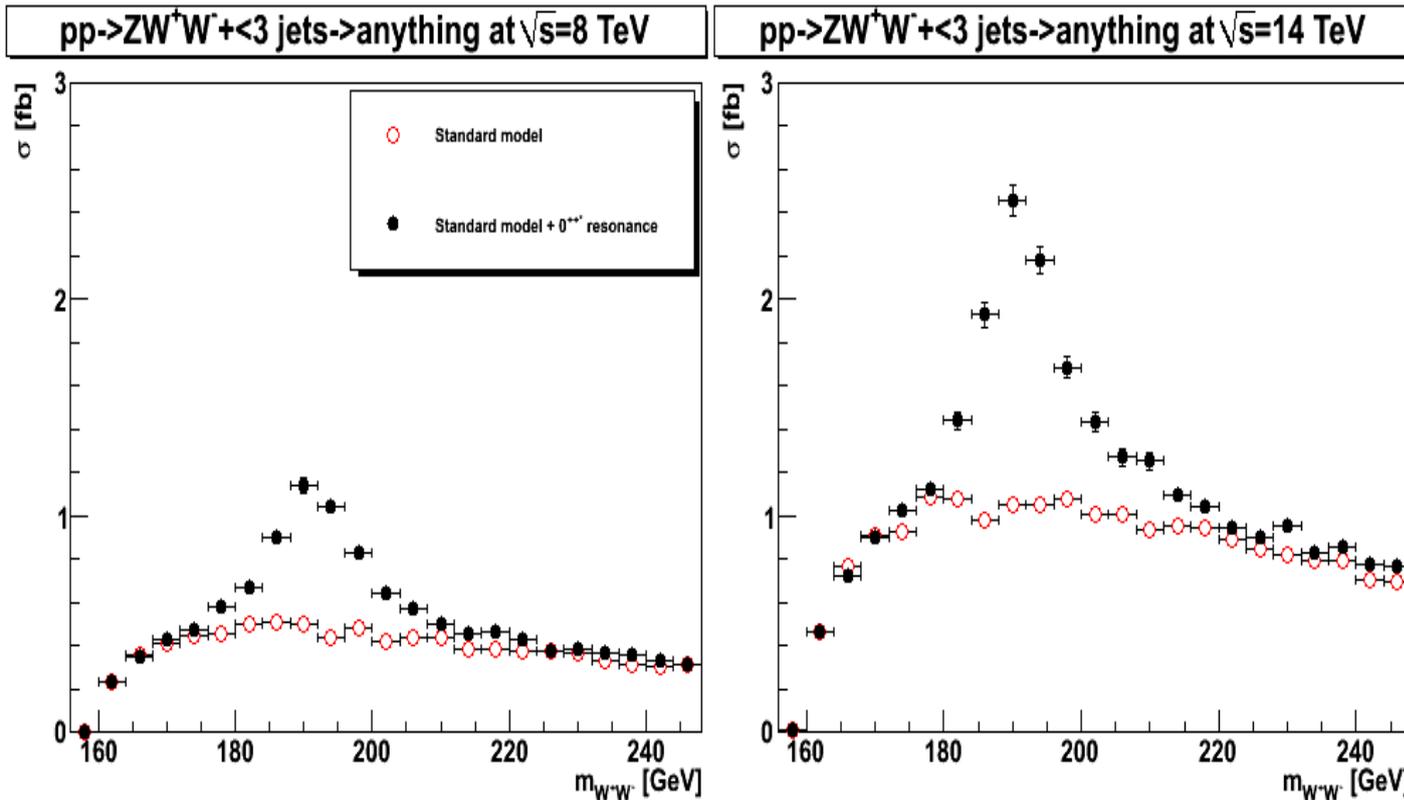
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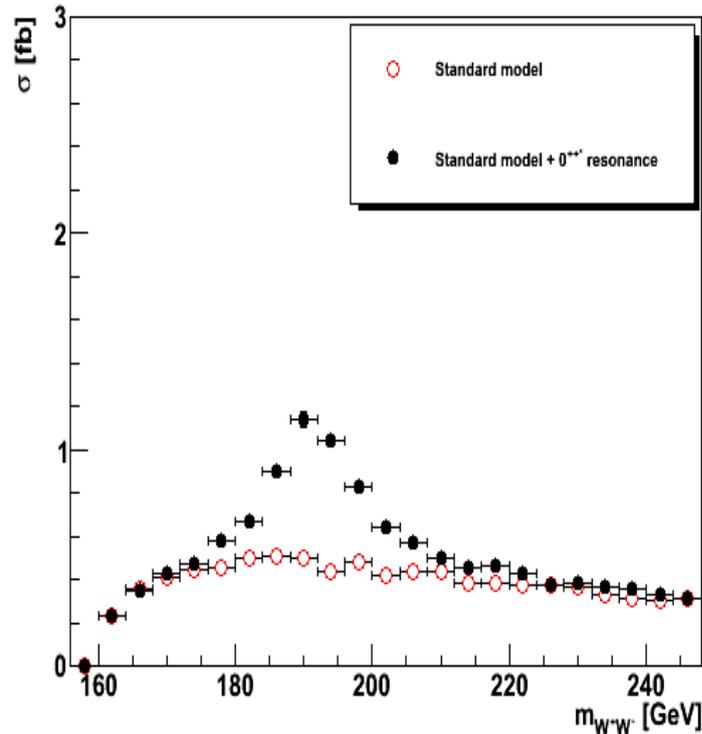
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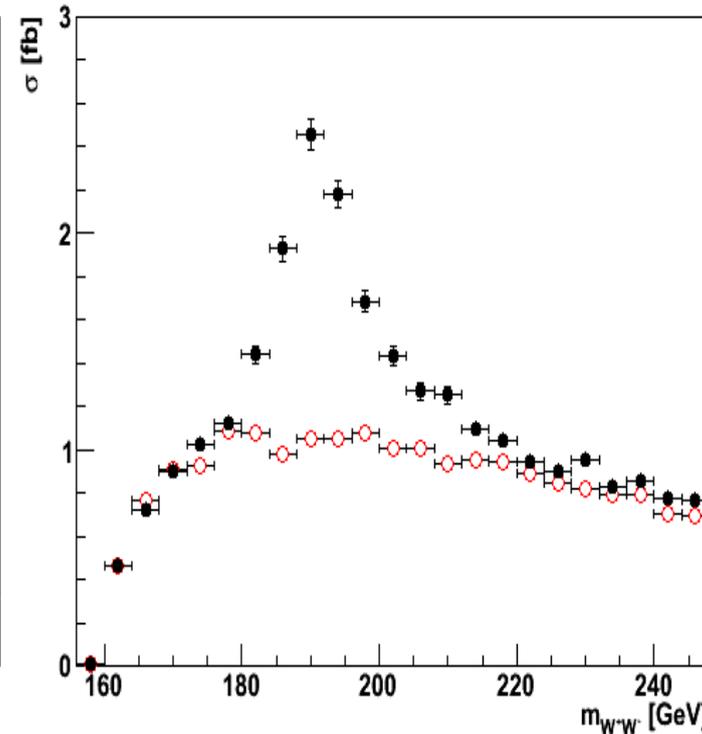
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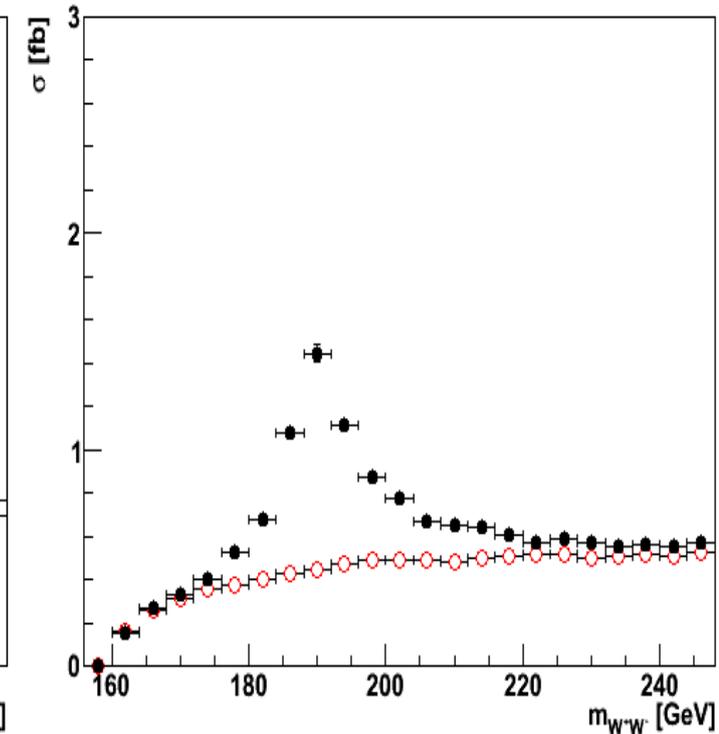
pp→ZW⁺W⁻+<3 jets→anything at √s=8 TeV



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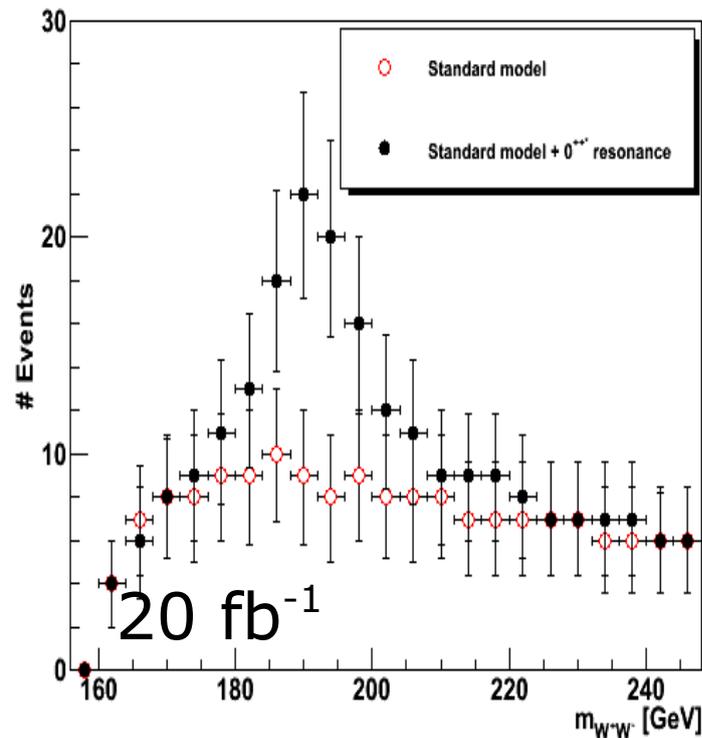
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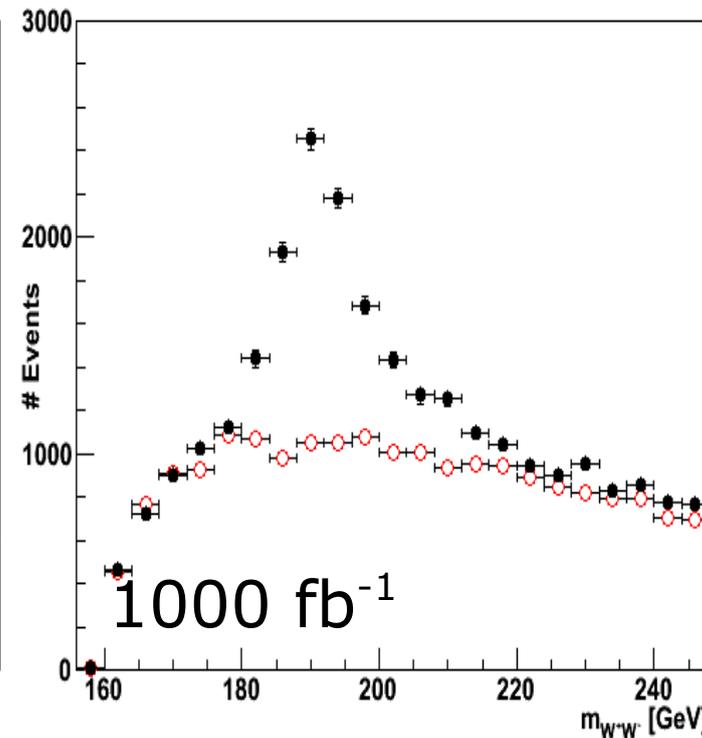
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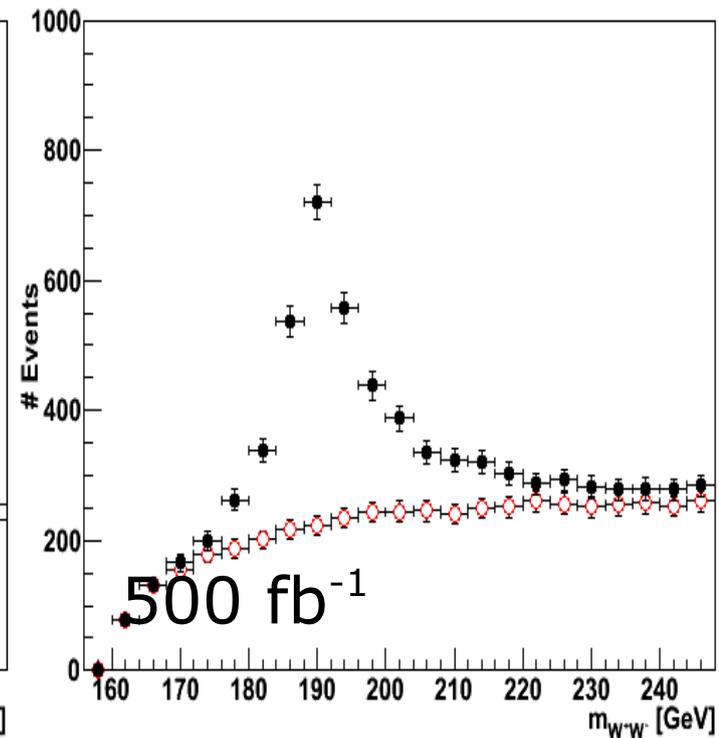
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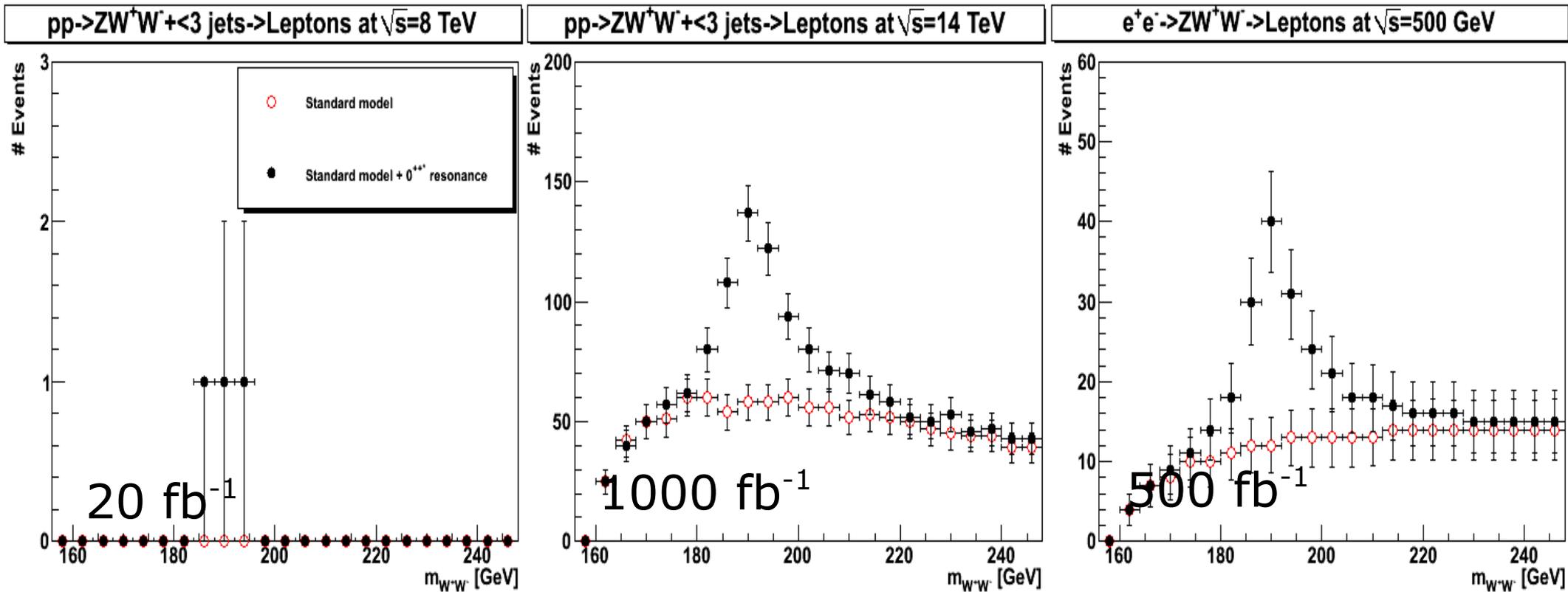
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- Interesting, alternative parameters: Talk by Wurtz