

# Study of thermal monopoles in lattice QCD

V.G. Bornyakov

IHEP, Protvino and ITEP, Moscow

LATTICE 2013  
JGU, Mainz              30.07.13

### Collaborators:

A.G. Kononenko (Moscow State University)

V.K. Mitrjushkin (JINR, Dubna and ITEP, Moscow)

### Motivation:

To study in SU(3) gluodynamics and QCD

- thermal monopole properties and their role in the quark-gluon plasma
- magnetic currents properties near the confinement-deconfinement transition

Dual superconductor - one of the most popular ideas about nature of confinement

t' Hooft '75, Mandelstam '76

Confinement in QCD is due to condensation of color-magnetic monopoles

Respective effective theory - dual Abelian Higgs model (dual superconductor)

Problem: how to determine monopoles in QCD

t' Hooft '81:

Partial gauge fixing

$$SU(N) \rightarrow U(1)^{N-1}$$

Very successful application of the MA gauge to define monopoles on a lattice

$$\sum_{c \neq 3,8} \left( \partial_\mu \delta_{ac} + \sum_{b=3,8} f_{abc} A_\mu^b(x) \right) A_\mu^c(x) = 0, \quad a \neq 3,8$$

extremums (over  $\textcolor{blue}{g}$ ) of the functional  $\mathcal{F}_{\text{MAG}}[A^g]$

$$\mathcal{F}_{\text{MAG}}[A] = \frac{1}{V} \int d^4x \sum_{a \neq 3,8} [A_\mu^a(x)]^2$$

Abelian projection:

$$A_\mu^a(x) T^a \rightarrow A_\mu^3(x) T^3 + A_\mu^8(x) T^8$$

on lattice

$$\begin{aligned} \mathcal{F}(U) &= \frac{1}{V} \sum_{x,\mu} (|U_\mu(x)^{11}| + |U_\mu(x)^{22}| + |U_\mu(x)^{33}|), \\ U_\mu(x) &\rightarrow u_\mu(x) \in U(1)^2 \end{aligned}$$

Magnetic currents definition:

$$j_\mu^{(a)} \equiv \frac{1}{4\pi} \epsilon_{\mu\nu\rho\sigma} \partial_\nu \bar{\Theta}_{\rho\sigma}^{(a)} = -\frac{1}{2} \epsilon_{\mu\nu\rho\sigma} \partial_\nu m_{\rho\sigma}^{(a)}, a = 1, 2, 3$$

satisfy the constraint

$$\sum_a j_\mu^{(a)}(x) = 0,$$

on any link  $\{x, \mu\}$  of the dual lattice

Magnetic currents form closed loops

Simulations details:

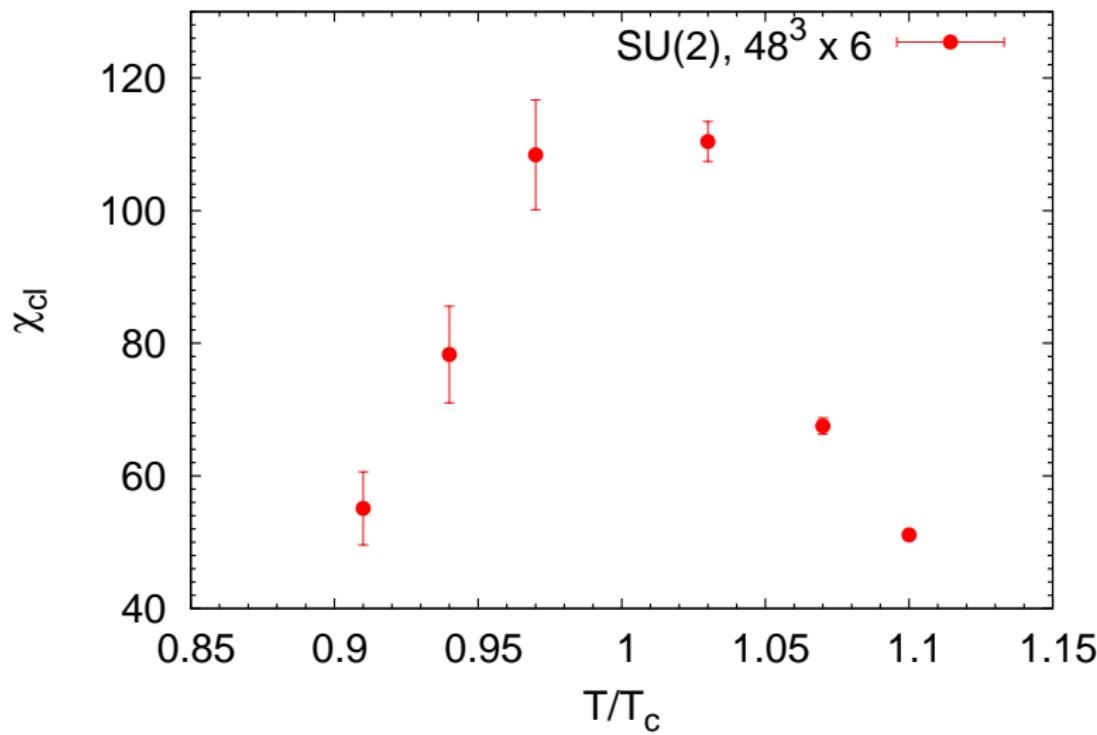
SU(3) gluodynamics, standard Wilson action, mostly  $32^3 \times 6$  lattices

$N_f = 2$  lattice QCD at  $T > 0$ , configurations produced by DIK collaboration, 2009

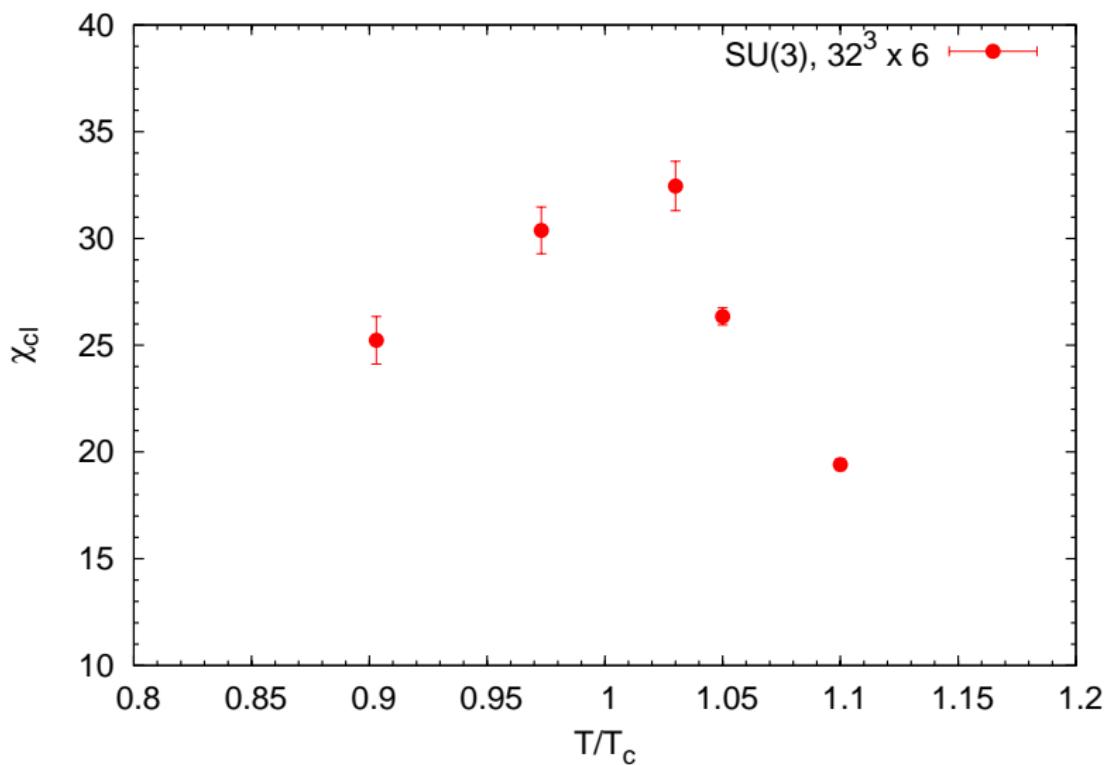
- Wilson action for the gauge field
- the non-perturbatively  $O(a)$  improved Wilson fermionic action  $S_F$ :

$$S_F = S_F^{(0)} - \frac{i}{2} \kappa g c_{sw} a^5 \sum_s \bar{\psi}(s) \sigma_{\mu\nu} F_{\mu\nu}(s) \psi(s)$$

- Lattice size  $12 \times (32)^3$
- Crossover at  $T_c = 200$  MeV,  $m_\pi = 400$  MeV
- Variation of temperature by variation of  $L_t$



Nonpercolating monopole cluster average size - 'susceptibility'  $\chi_{cl}$



Same for SU(3)

There are proposals suggesting that the color-magnetic monopoles contribution can explain strong coupling property of QGP near transition

Chernodub and Zakharov 2006, Liao and Shuryak 2006,

Chernodub and Zakharov:

Thermal monopoles are related to clusters of magnetic currents wrapped in  $T$  dimension

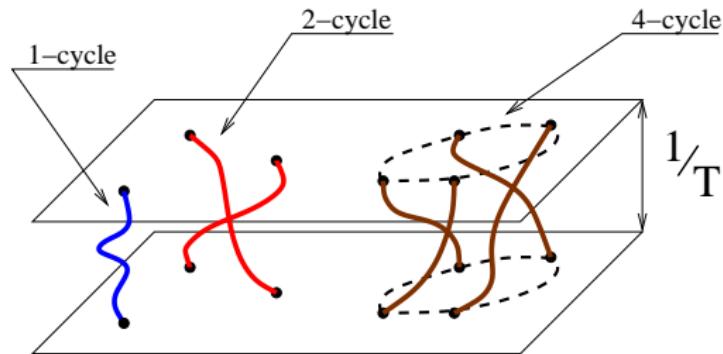


Figure from D'Alessandro, D'Elia and Shuryak, 2010

Wrapping number for given cluster:

$$N_{wr}^a = \frac{1}{3L_t} \sum_{j_4^a(x) \in \text{cluster}} j_4^a(x)$$

$$\rho = \frac{\langle \sum_{\text{clusters}, a} |N_{wr}^a| \rangle}{3L_s^3 a^3}$$

First lattice study in  $SU(2)$  by VB, Mitrjushkin, Muller-Preussker ,  
1992

Comprehensive lattice study in  $SU(2)$  by D'Alessandro and D'Elia 2007

Subsequent work, also in  $SU(2)$ : VB, Braguta, 2011; VB, Kononenko,  
2012

First results for  $SU(3)$  and QCD: VB, Kononenko, Mitryushkin,  
presented at Confinement X, 2012

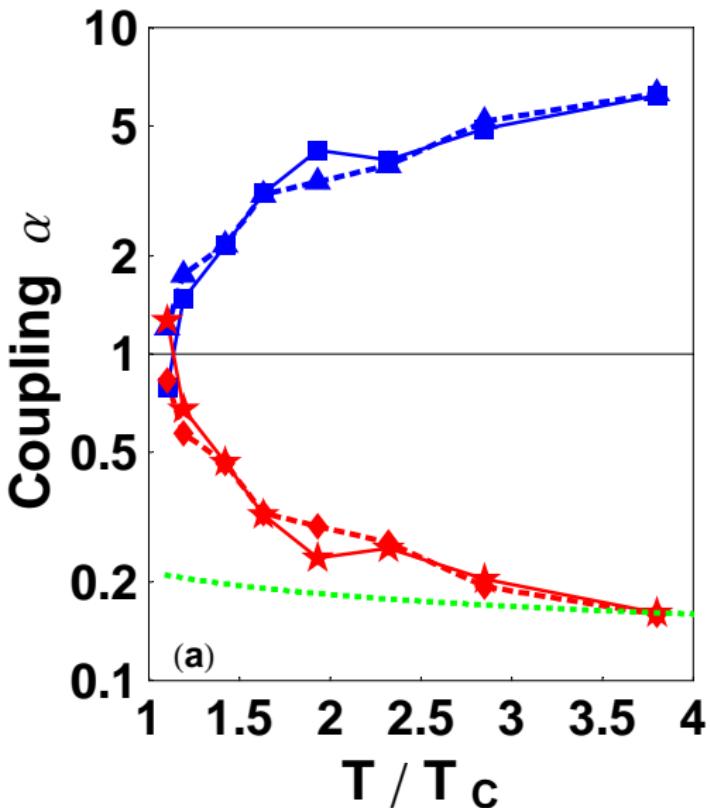
## Liao and Shuryak

### Magnetic scenario:

- magnetic monopoles are weakly interacting ( $\alpha_M \sim 1/\alpha_E$ ) near  $T_c$  and are dominating fluctuations
- strongly influence QGP property, in particular reduce its viscosity

Alternative approach to study of monopoles: Classical molecular dynamics simulations for system with mixture of magnetic and electric charges

- Remarkably, good qualitative agreement with lattice results for density-density correlation functions
- Magnetic coupling  $\alpha_M$  was computed from (lattice) correlation functions
- $\alpha_M$  increases with temperature

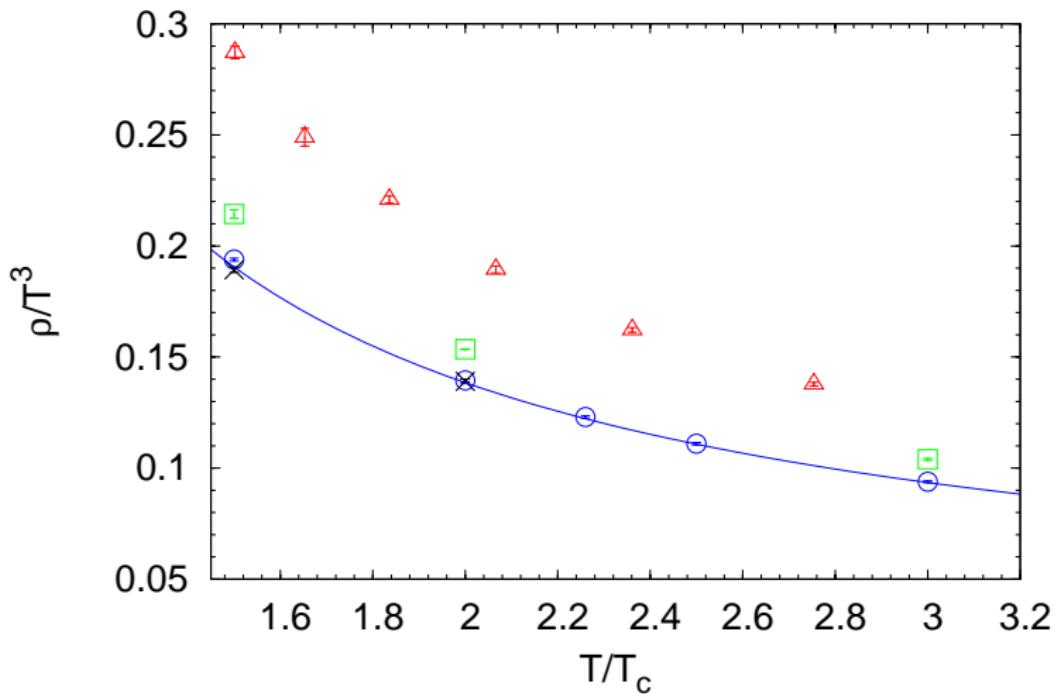


$\alpha_M$  (blue symbols) extracted by Shuryak and Liao from lattice data  
obtained by D'Alessandro and D'Elia

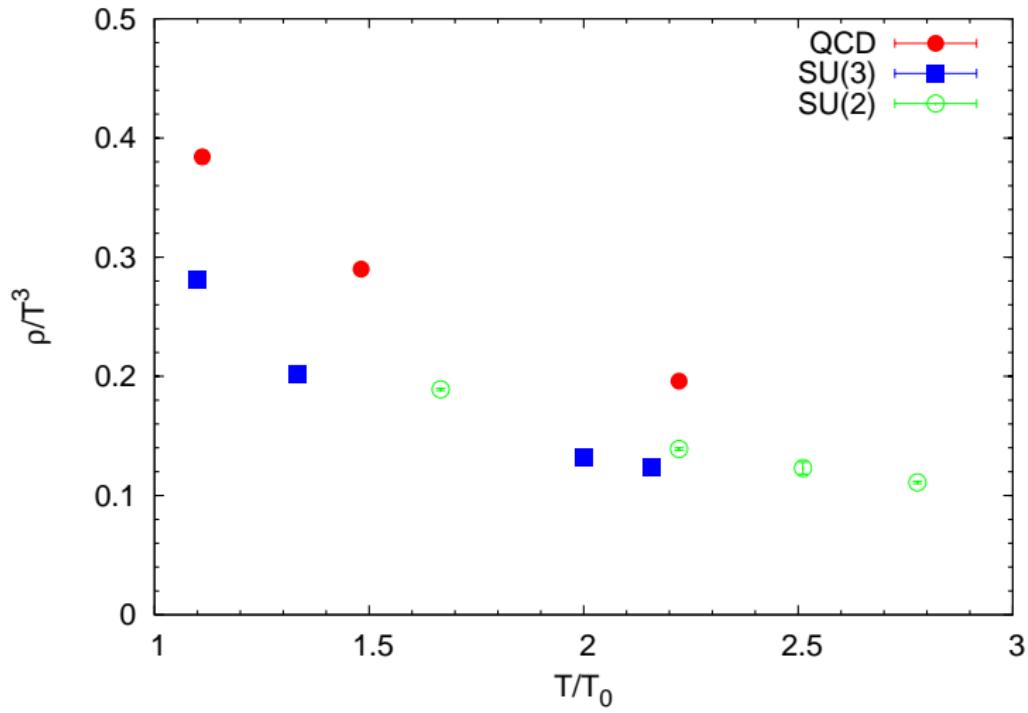
## Coulomb plasma parameter

$$\Gamma = \alpha_m \left( \frac{4\pi\rho}{3T^3} \right)^{1/3}$$

- $\Gamma > 1$ , i.e. strongly coupled plasma
- $\Gamma$  increases up to about 5 with increasing temperature



Total thermal monopoles density in  $SU(2)$

Total thermal monopoles density  $\rho$  vs  $T/T_0$

## Bose-Einstein condensation of the thermal monopoles

First study in SU(2) theory by D'Alessandro, D'Elia and Shuryak, 2010

a trajectory wrapping  $k$  times in a time direction represents a set of  $k$  monopoles permuted cyclically  
for non-relativistic noninteracting bosons

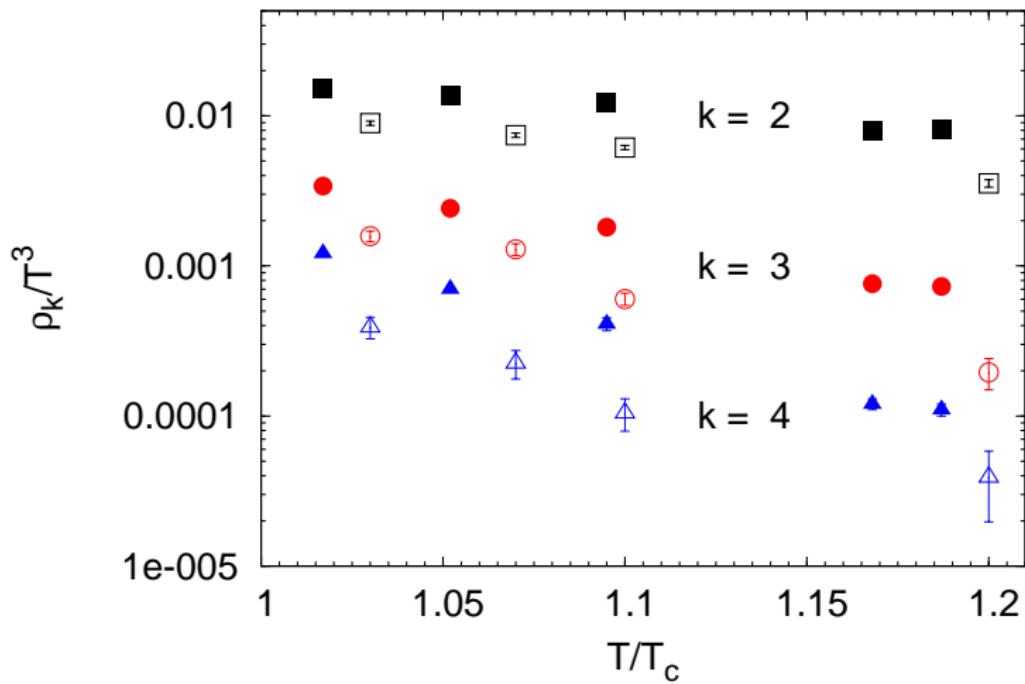
$$\rho_k = \frac{e^{-\hat{\mu}k}}{\lambda^3 k^{5/2}} \quad (1)$$

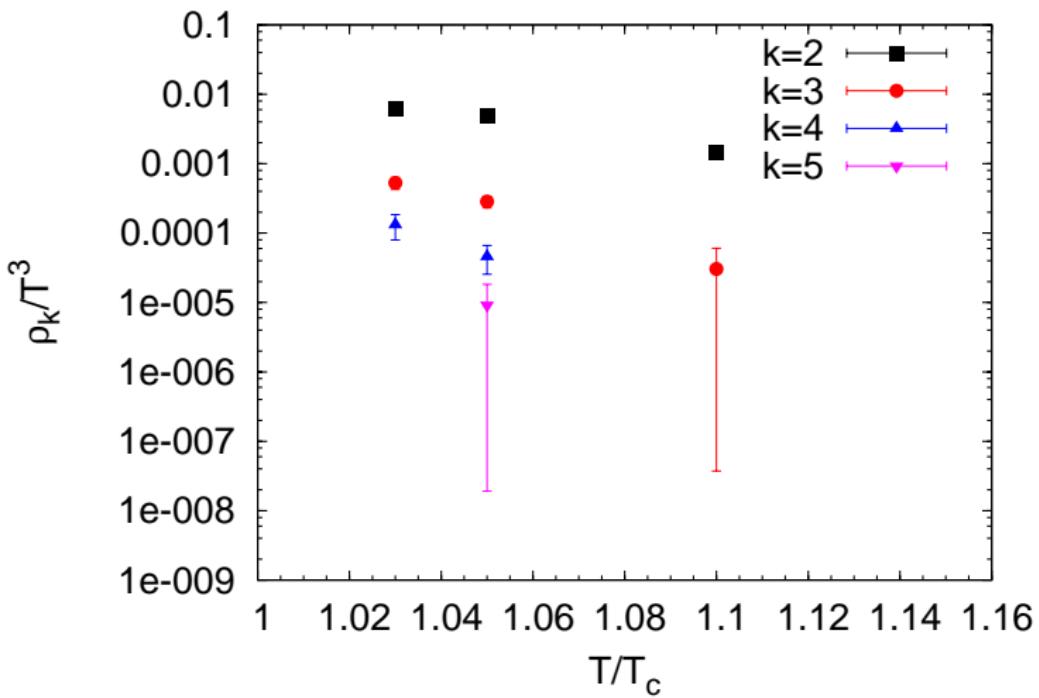
$\hat{\mu} \equiv -\mu/T$  is a chemical potential

$\lambda$  is the De Broglie thermal wavelength

the condensation temperature  $T_{BEC}$  is determined by the vanishing of the chemical potential

$T_{BEC} \approx T_c$       D'Alessandro, D'Elia and Shuryak, 2010  
 confirmed in VB, Kononeko, 2012

Thermal monopoles density  $\rho_k$  vs  $T/T_c$  for  $SU(2)$



Thermal monopoles density  $\rho_k$  vs  $T/T_c$  for  $SU(3)$

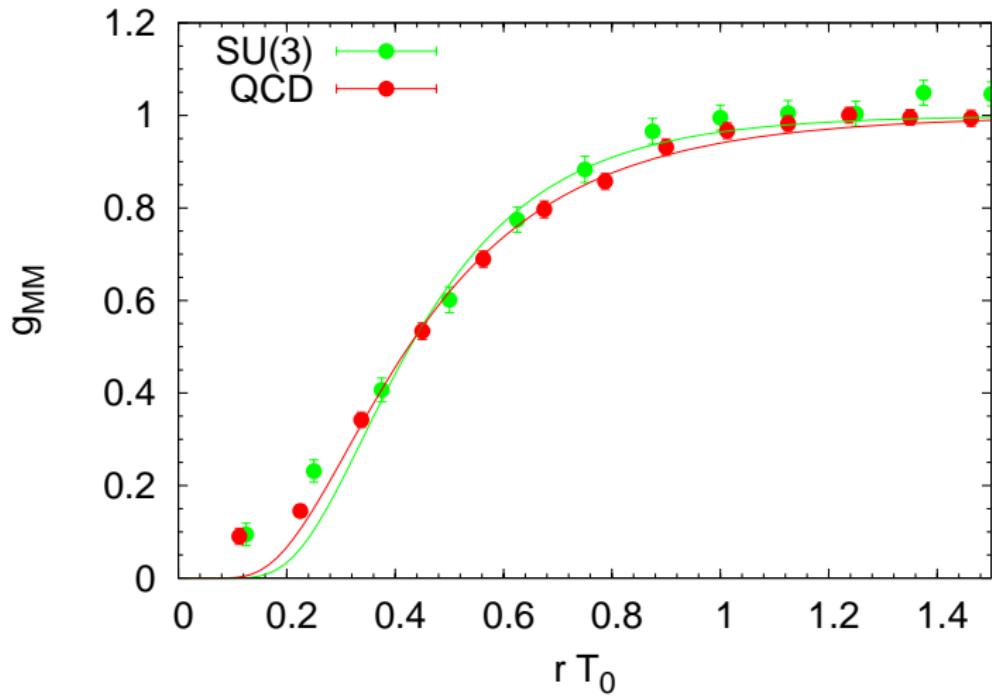
## Thermal monopole interactions

$$g_{MM}(r) = \frac{\langle \rho_M^a(0)\rho_M^a(r) \rangle}{2\rho_M^b\rho_M^b} + \frac{\langle \rho_A^a(0)\rho_A^a(r) \rangle}{2\rho_A^b\rho_A^b}$$

$$g_{AM}(r) = \frac{\langle \rho_A^a(0)\rho_M^a(r) \rangle}{2\rho_A^b\rho_M^b} + \frac{\langle \rho_M^a(0)\rho_A^a(r) \rangle}{2\rho_A^b\rho_M^b}$$

$$g_{MM,AM}(r) = e^{-U(r)/T}$$

$$U(r) = \frac{\alpha_m}{r} e^{-m_D r}$$



Thermal monopoles correlation functions for  $T/T_c = 2$

Table of results for  $T/T_c = 2$ 

	$\alpha_M$	$m_D/T$	$\Gamma$
$SU(2)$	2.61(15)	1.75(12)	1.95(16)
$SU(3)$	2.8(6)	1.8(2)	2.2(4)
QCD	1.4(2)	1.8(1)	1.4(2)

## Conclusions

We present new evidence on the percolation transition at  $T_c$  in  $SU(3)$  gluodynamics

Our numerical results indicate

- Density of thermal monopoles in  $SU(3)$  gluodynamics is similar to that in  $SU(2)$  gluodynamics
- In QCD it is substantially higher
- qualitative confirmation of the Bose-Einstein condensation in  $SU(3)$  gluodynamics
- Magnetic coupling  $\alpha_m$  and screening mass  $m_D/T$  in  $SU(3)$  are close to those in  $SU(2)$
- $\alpha_m$  in QCD is lower by factor 2,  $m_D/T$  is somewhat lower