

Surface operator study in $SU(2)$ gauge field theory

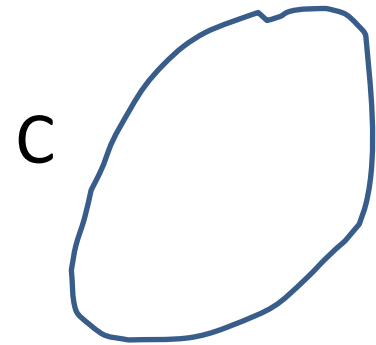
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Line operator

- Wilson loop operator:

$$W_C = \text{Tr} \left(P e^{ig \oint_C A dc} \right)$$



Confinement phase: area law

$$W_C \propto e^{-\sigma S(C)}$$

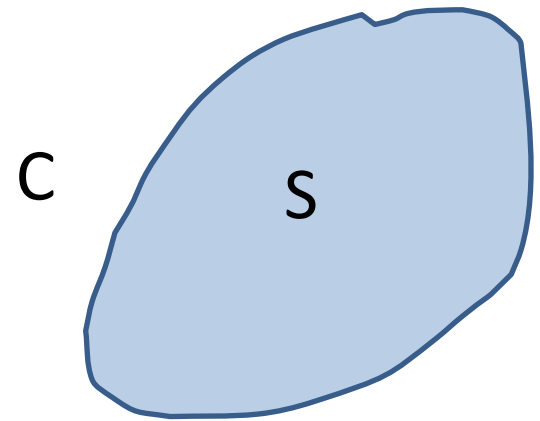
Deconfinement phase: perimeter law

$$W_C \propto e^{-kp(C)}$$

Surface operators

- For a general gauge group

$$W_S = \text{Tr} \left(P e^{ig \int_S F d\sigma} \right)$$



- E. Witten, S. Gukov:

4D SYM Theory, spatial surface operator

Area law at low T: $W_S \propto e^{-\sigma S}$

Volume law high T: $W_S \propto e^{-\gamma V}$

From surface to lines

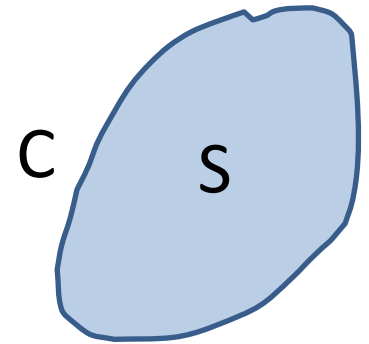
- In the limit $\beta \rightarrow 0$ the 4D SYM theory reduces to a pure (non- supersymmetric) three-dimensional Yang-Mills theory on S .
- In this limit, a temporal surface operator turns into a line operator (supported on γ) in the 3D theory.
- Therefore, surface operators in the four-dimensional gauge theory exhibit volume (resp. area) law whenever the corresponding line operators in the 3D theory exhibit area (resp. circumference) law.

S. Gukov, E. Witten

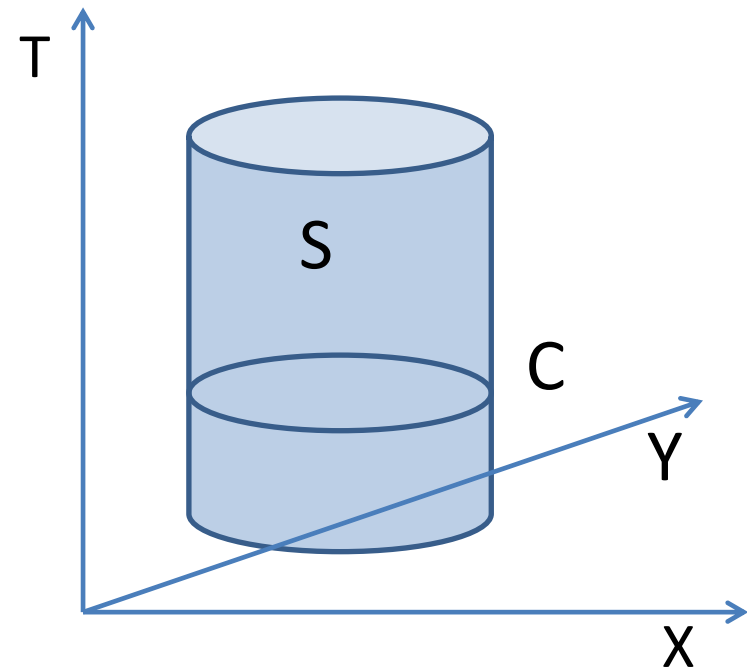
Line – Surface operators correspondence

- In abelian gauge field theory

$$\text{Tr} \left(Pe^{ig \oint_C A dc} \right) = \text{Tr} \left(Pe^{ig \int_S F d\sigma} \right)$$

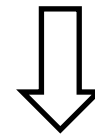


- In general case:



Deconfinement phase

Spatial Wilson loop: perimeter law



Temporal surface operator: area law

Calculation within SU(2) LQCD

- Surface operator on lattice:

$$W_S = \text{Re} S \prod e^{i\theta_p} \quad \theta_p = g \int_S F d\sigma$$

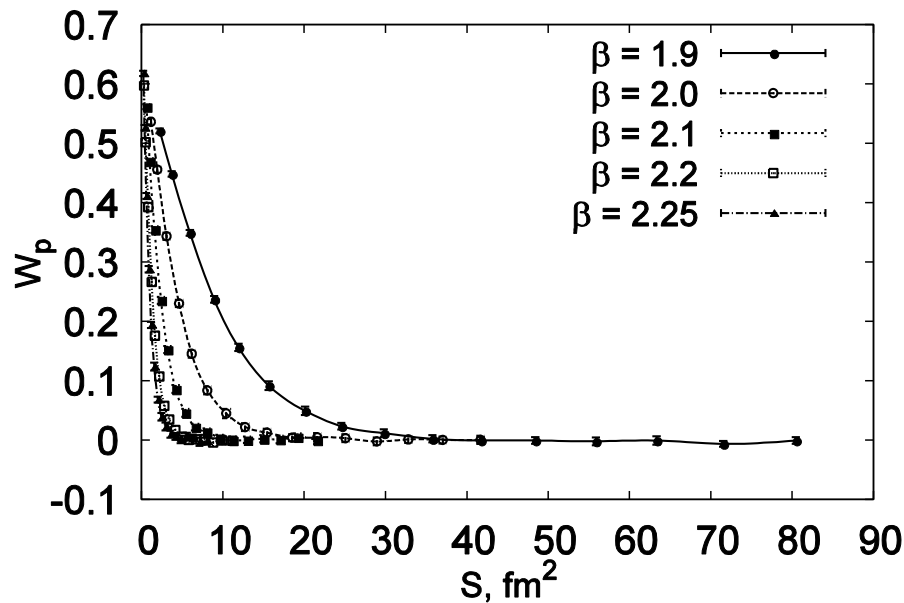
- SU(2) pure gauge:

$$F_p = \hat{1} \cos \theta_p + i n_i \sigma_i \sin \theta_p$$

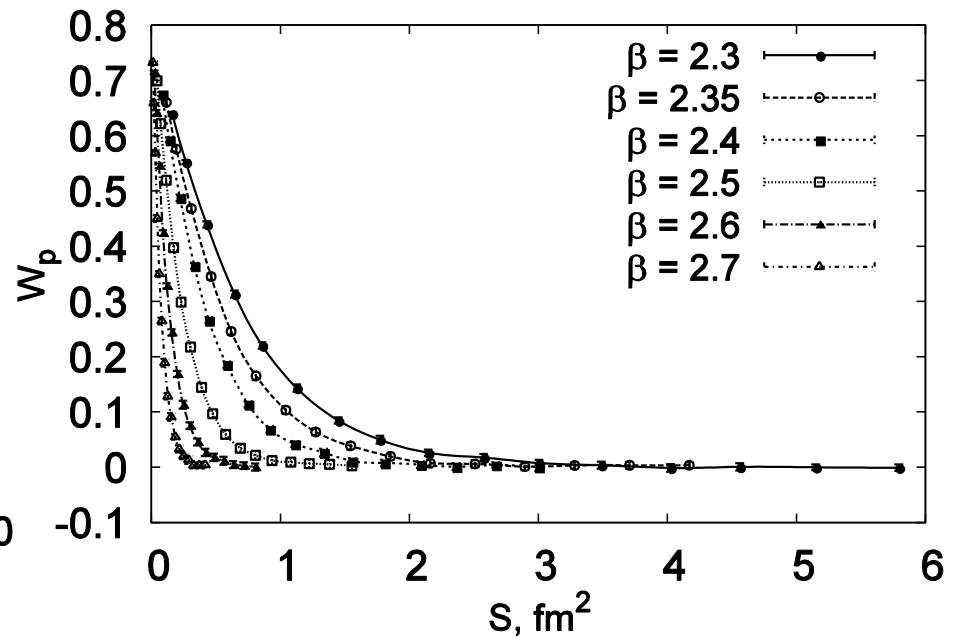
$$\theta_p = \arccos \left(\frac{1}{2} \text{Tr} F_p \right)$$

Surface operator calculation

Confinement phase



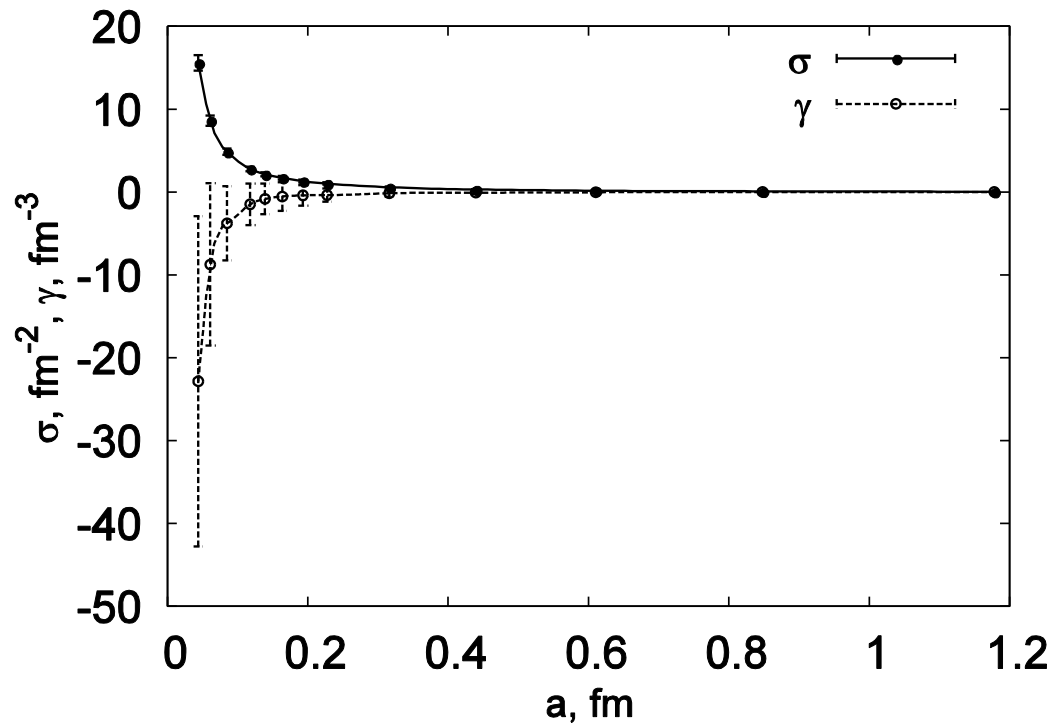
Deconfinement phase



Surface operator parameterization:

$$W_S = C e^{-\sigma S - \gamma V}$$

Lattice spacing dependence



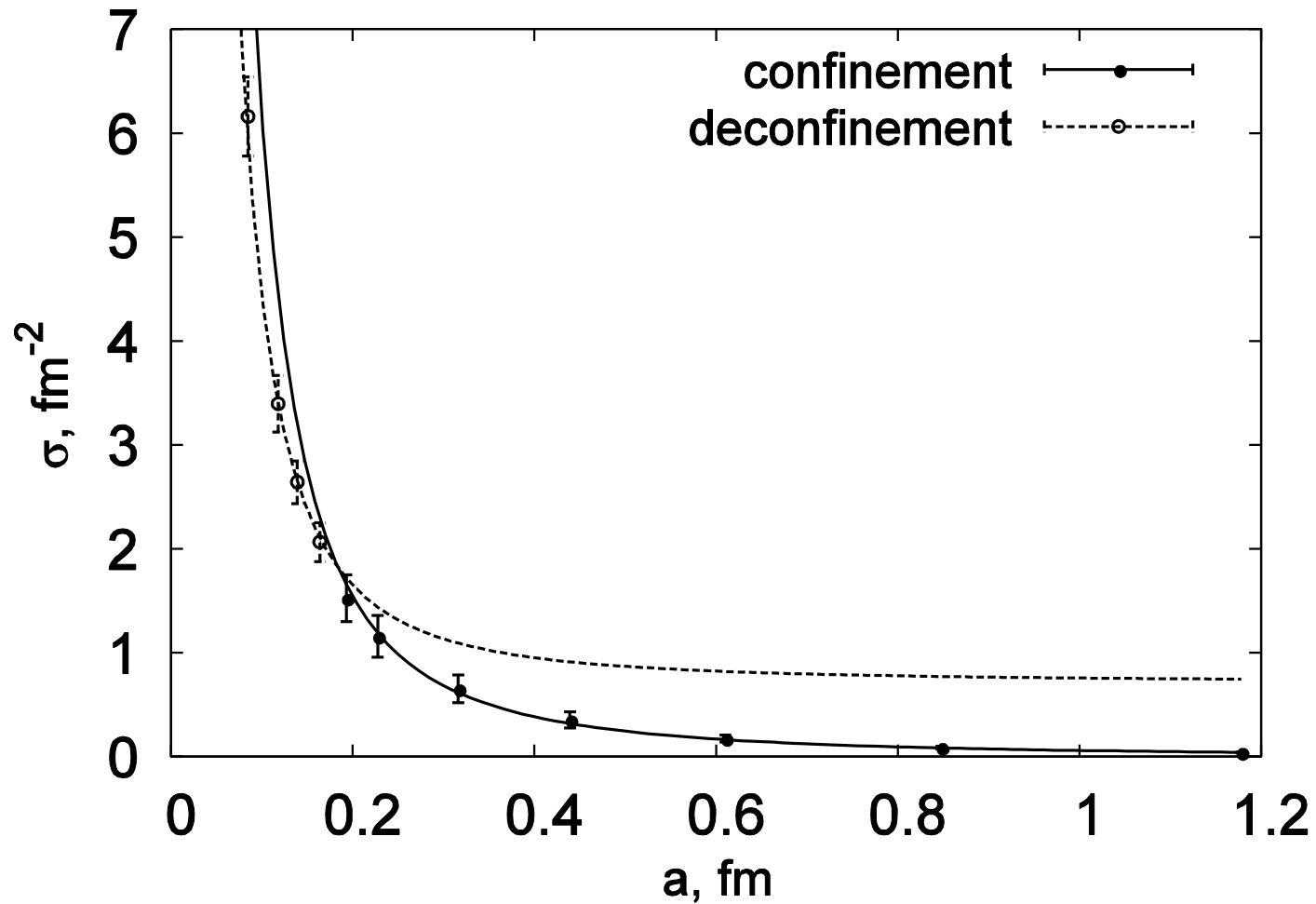
- Dipole self-energy -> area coefficient divergence:

$$\sigma(a) = \sigma_{ph} + \sigma_{div}/a^2$$

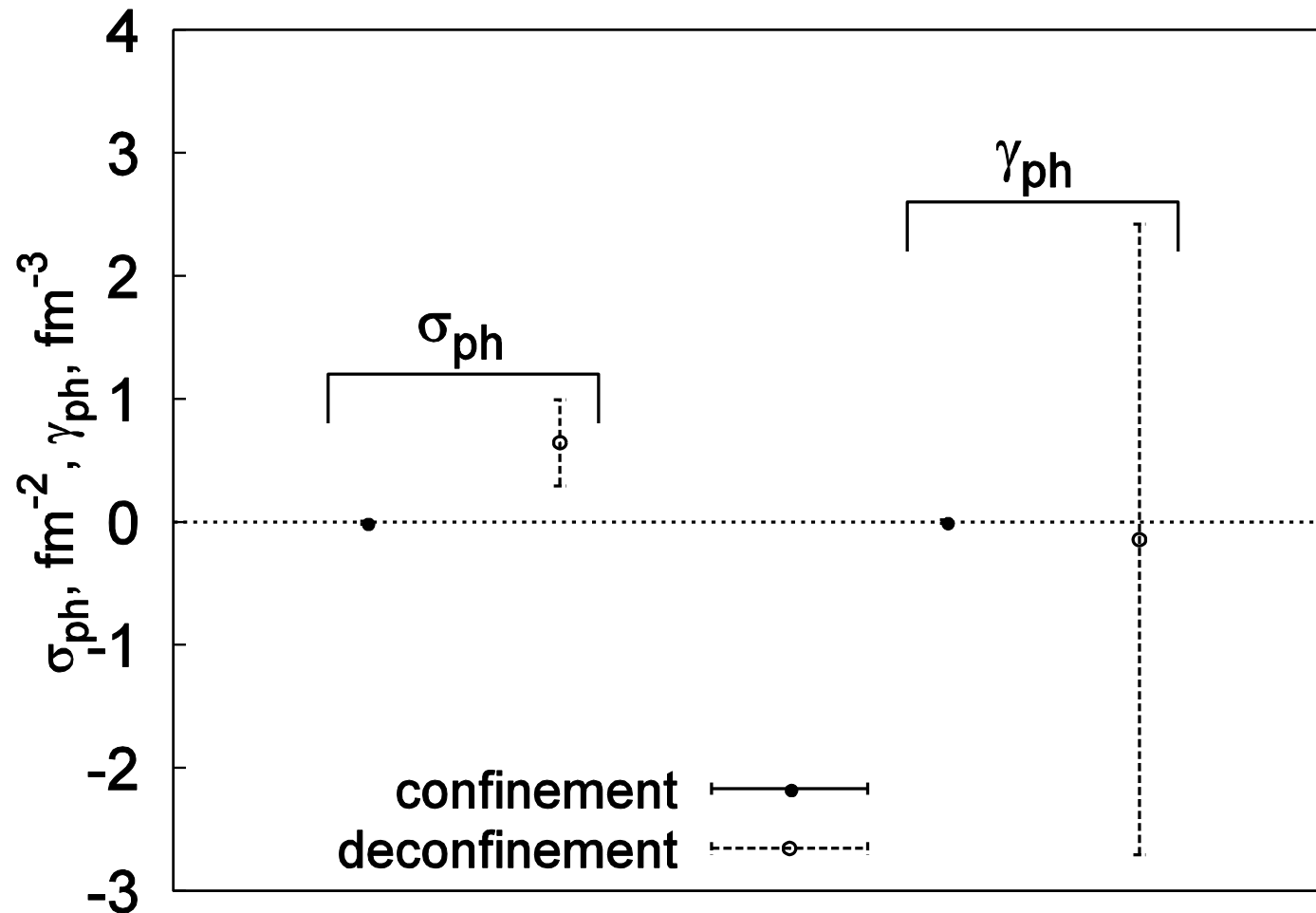
- Volume coefficient divergence:

$$\gamma(a) = \gamma_{ph} + \gamma_{div}/a^3$$

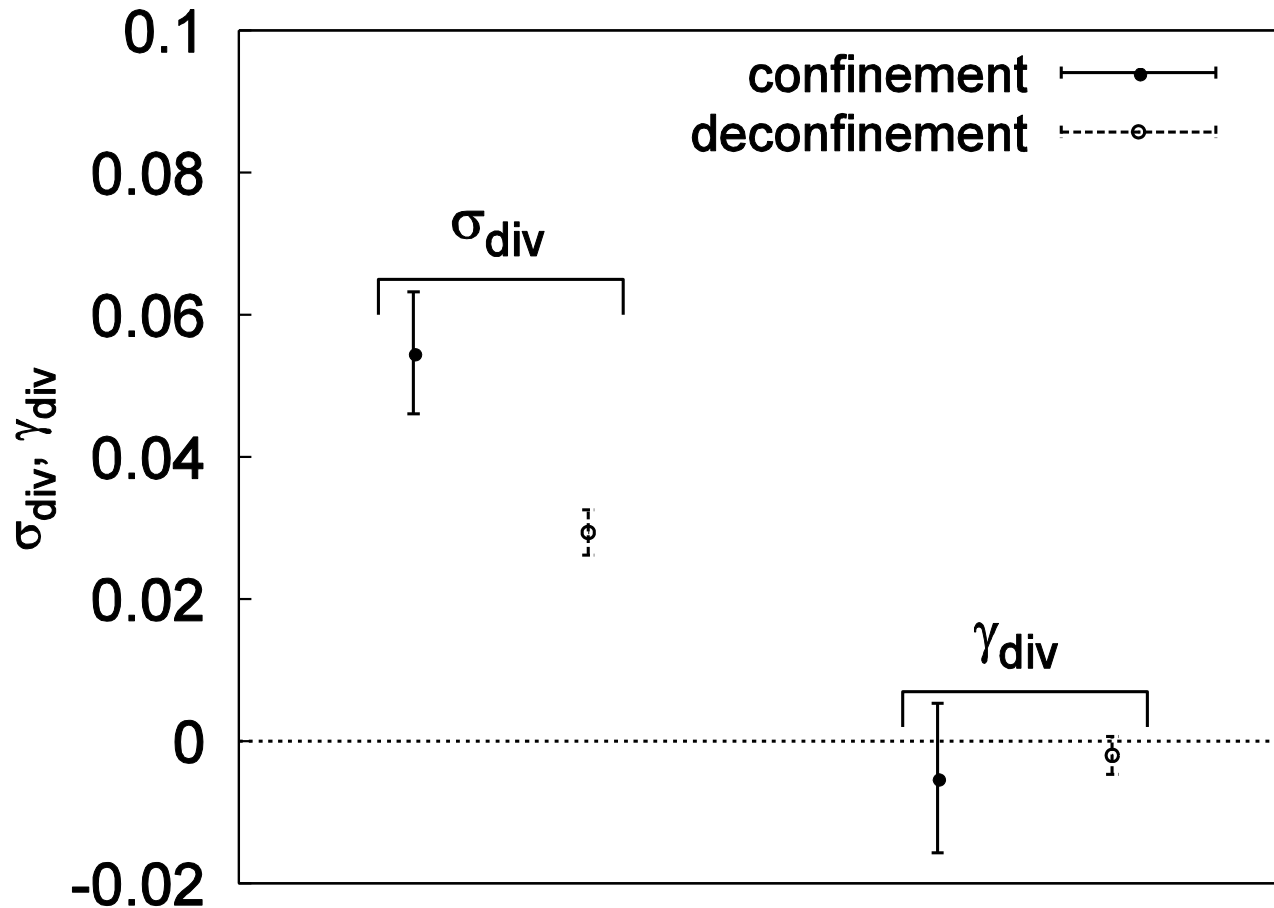
Extraction of the S dependence



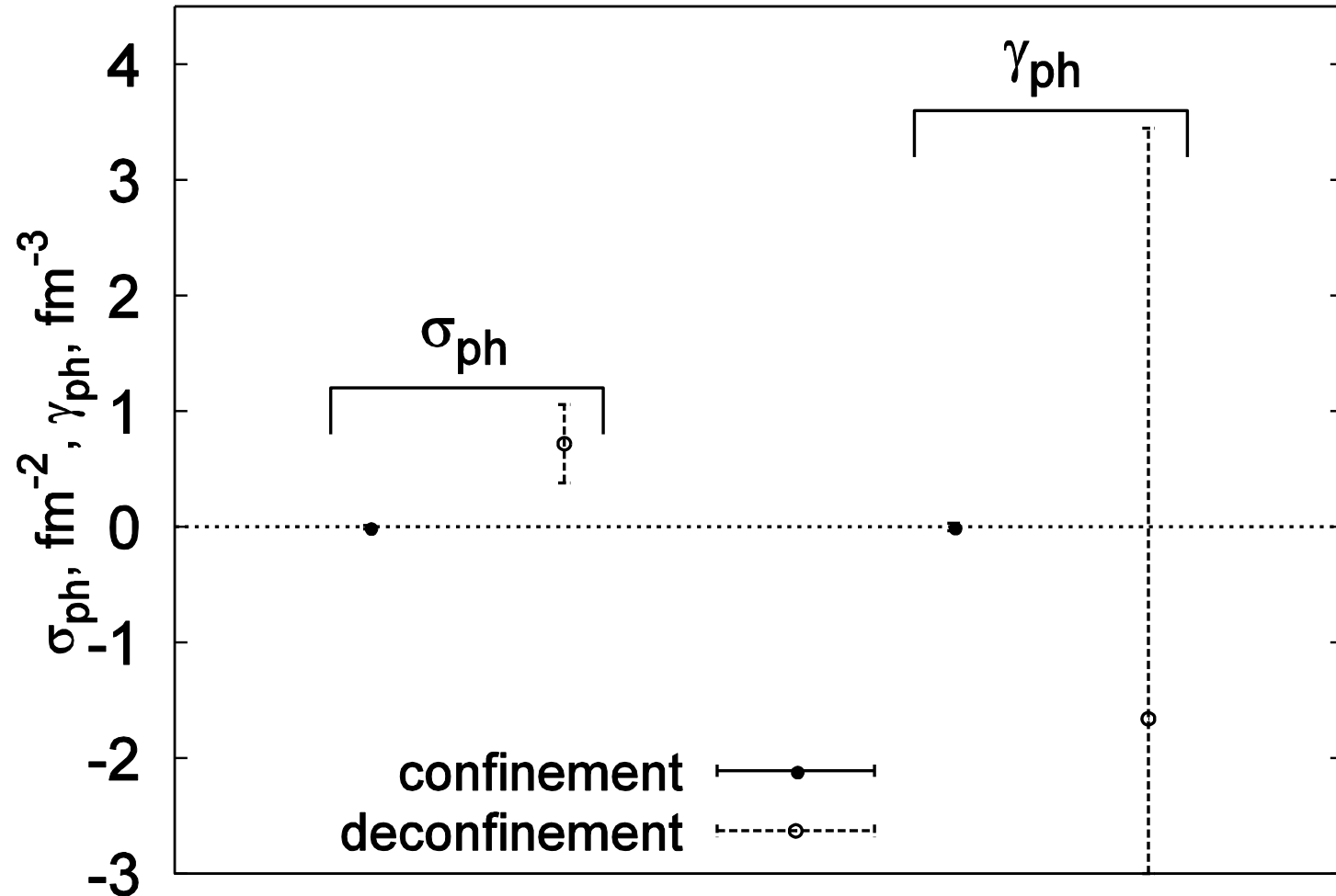
Temporal surface



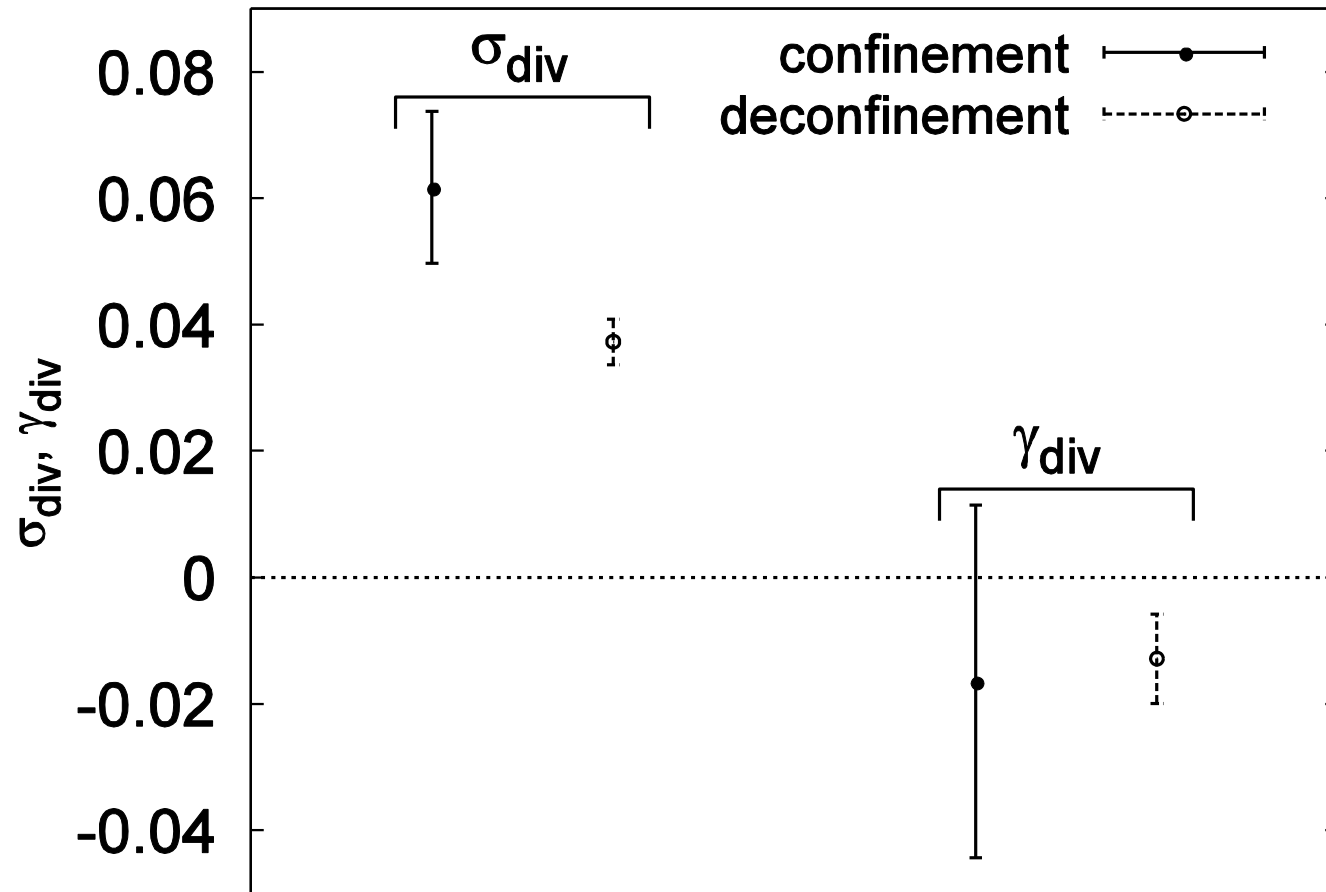
Temporal surface (divergent part)



Spatial surface



Spatial surface (divergent part)



Conclusion

- Area law of the temporal surface operator corresponds to the perimeter law of the Wilson loop
- Temporal surface operator has no volume dependence
- Volume dependence of the spatial surface needs more precise study