

$$S_P^\mu[U_{\mathbf{x}},U_{\mathbf{x}}^\dagger]=S_P^{\mu=0}[e^{N_t\mu}U_{\mathbf{x}},e^{-N_t\mu}U_{\mathbf{x}}^\dagger]$$