

$$S_P^\mu[U_x, U_x^\dagger] = S_P^{\mu=0}[e^{N_t\mu}U_x, e^{-N_t\mu}U_x^\dagger]$$